

'Apps' Biologicas

Natalio Krasnogor
Newcastle University

Twitter: @NKrasnogor

<http://homepages.cs.ncl.ac.uk/natalio.krasnogor/>



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Contenido

- Introduccion a la BioComputacion
- 'Apps' biologicas: como programar organismos vivos (modelos, herramientas, ejemplos)
- Infraestructuras informaticas para el modelado 3D de colonias bacterianas

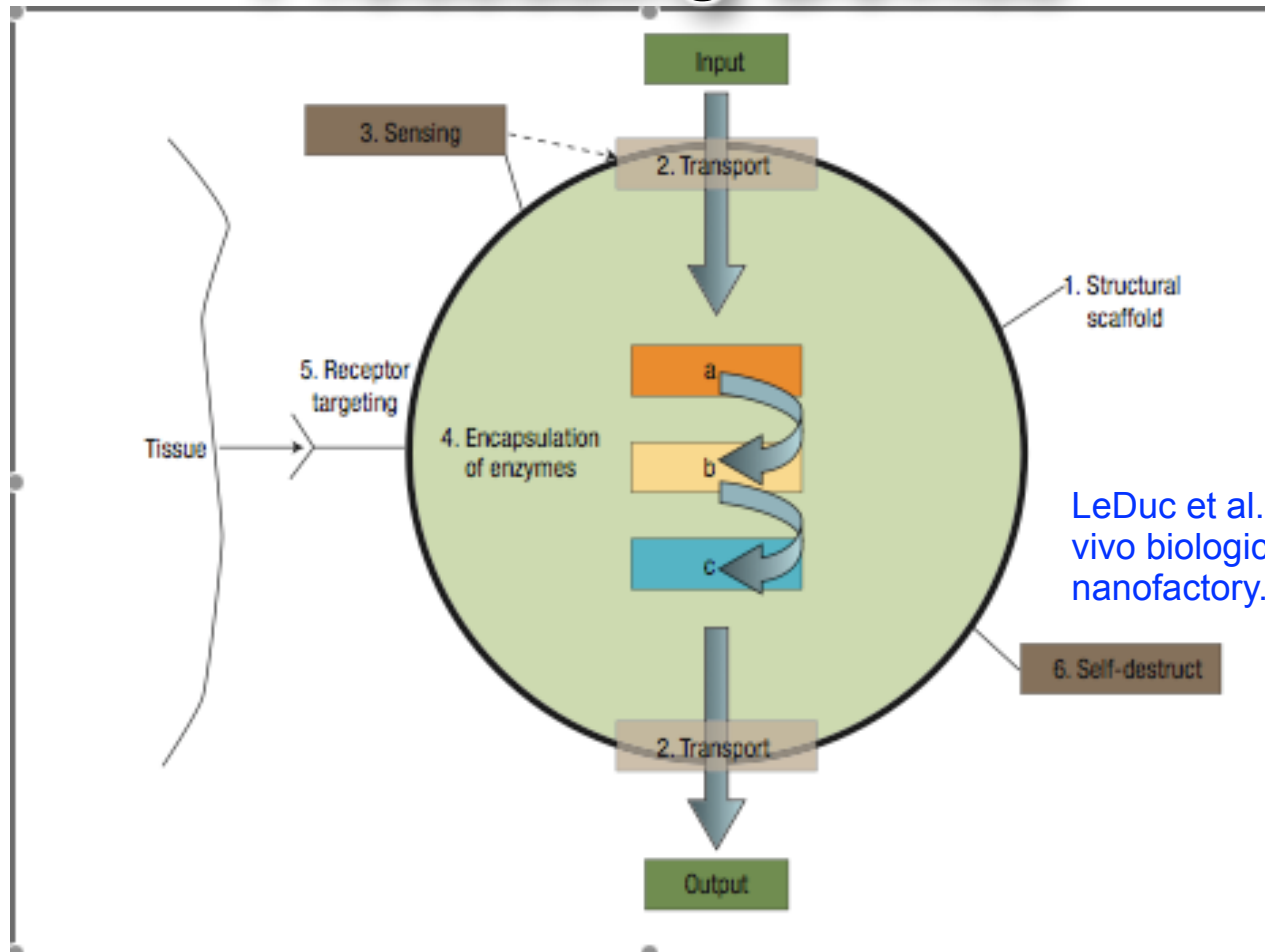
Outline

- The cell as a Computing Device for Biocomputing
- P Systems for Representing Cellular Computation
- Examples of Biocomputation
- Conclusions

Outline

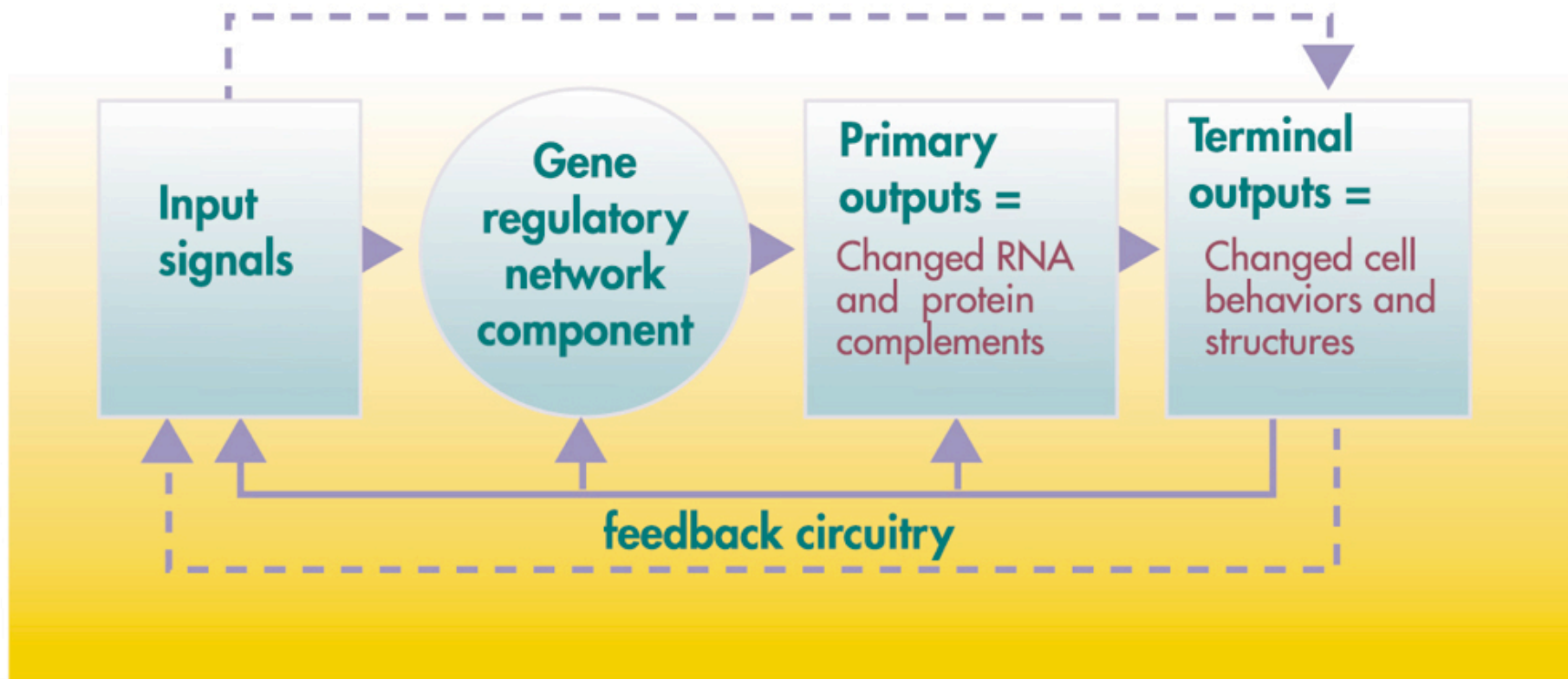
- The cell as a Computing Device for Biocomputing
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The Cell as an Information Processing Device



LeDuc et al. Towards an in vivo biologically inspired nanofactory. Nature (2007)

The Cell as an Intelligent (Evolved) Machine



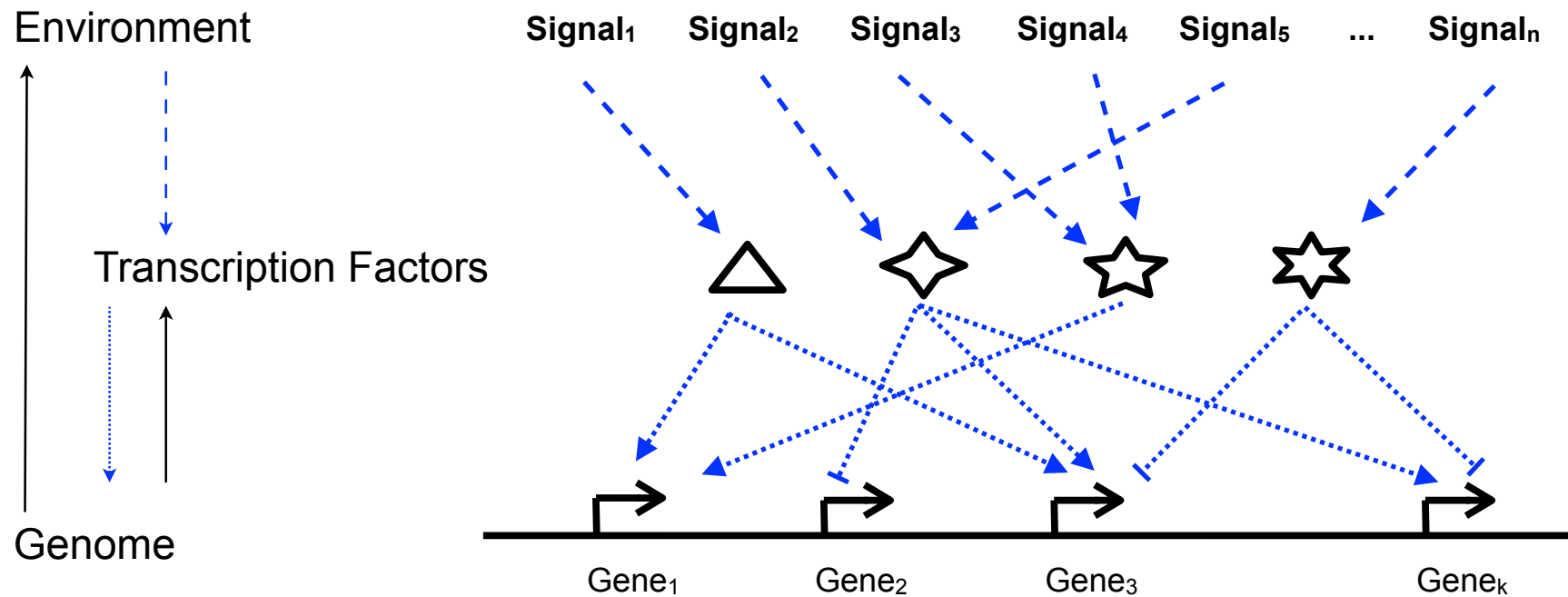
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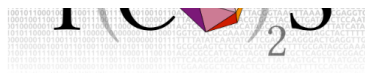
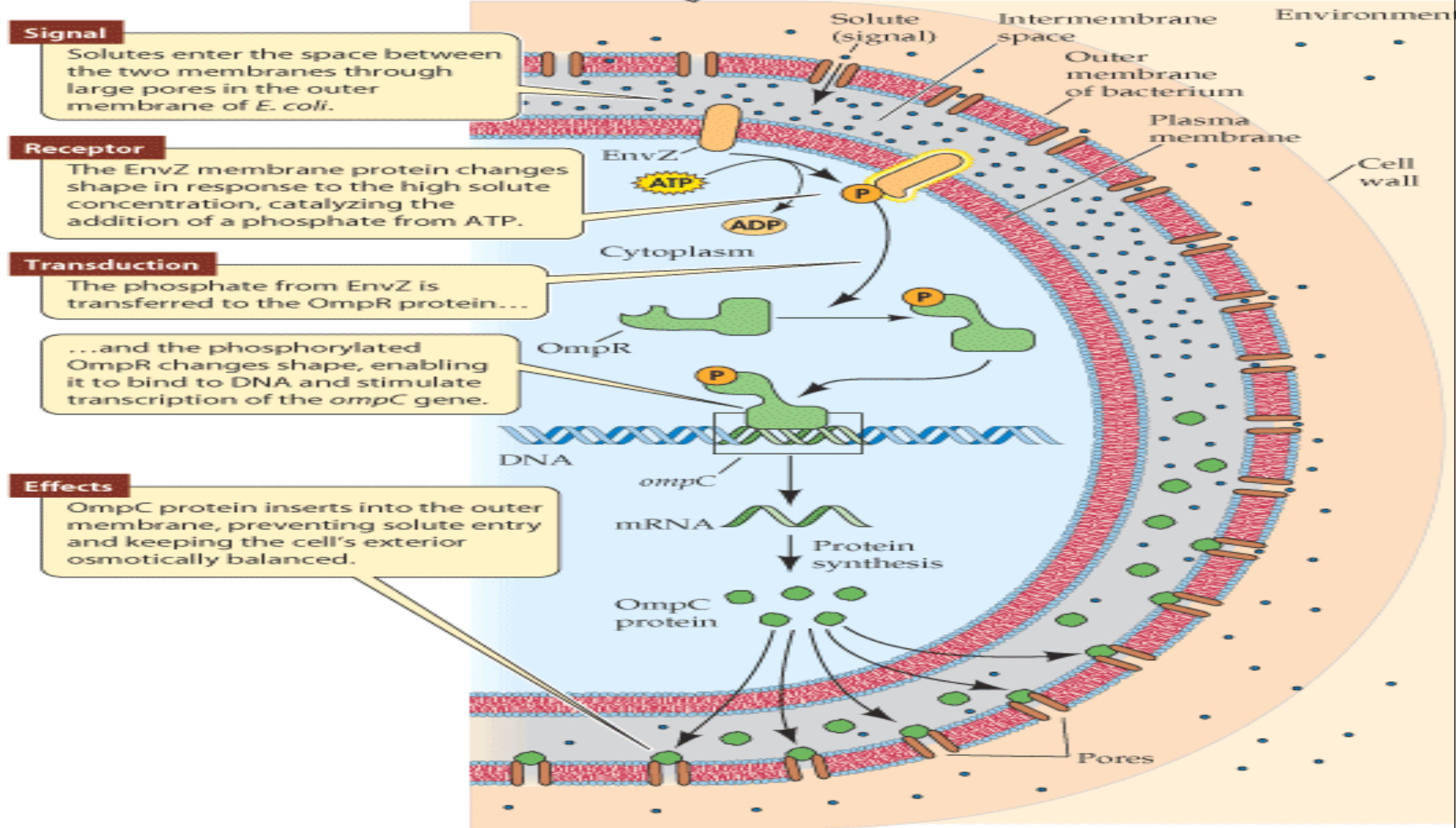
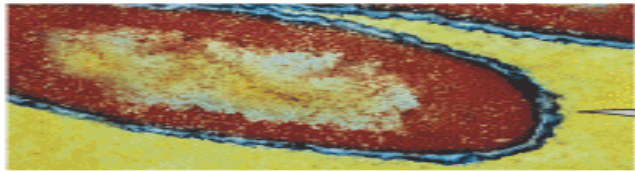


Amir Mitchell, et al., Adaptive prediction of environmental changes by microorganisms. Nature June 2009.

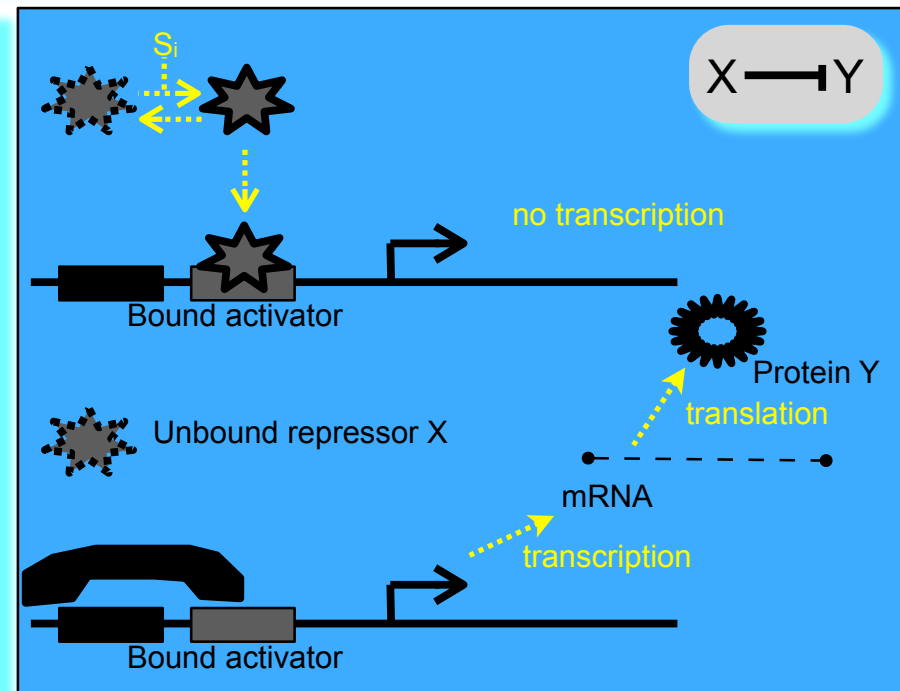
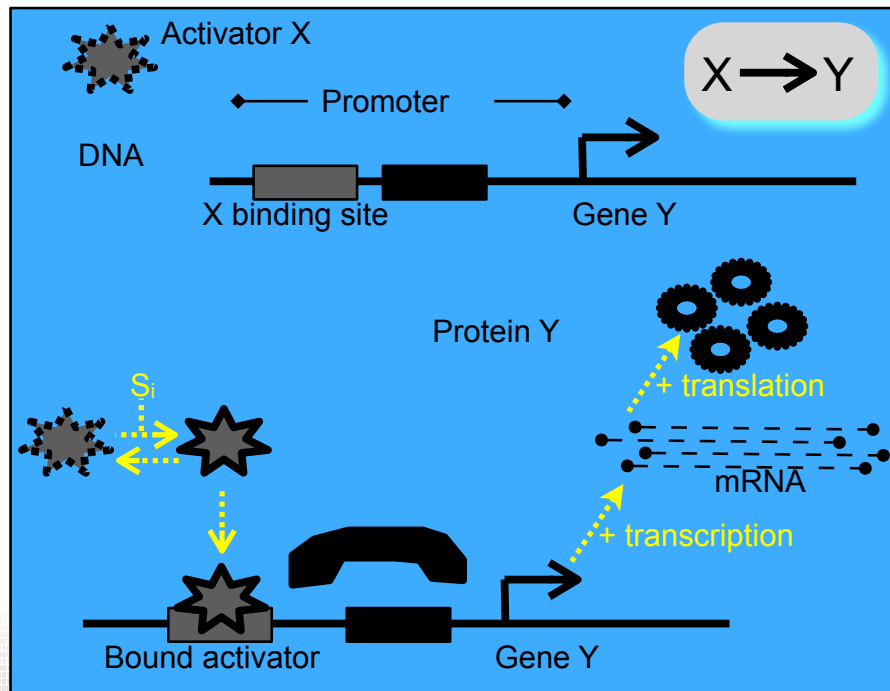
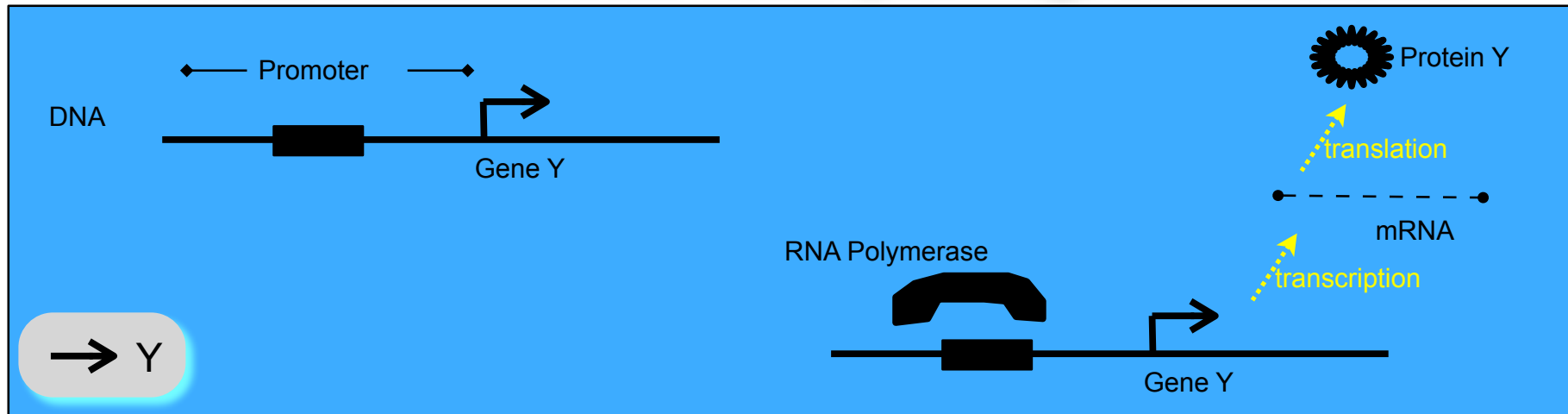


Transcription Networks





The Basic Unit: A Gene's Transcription Regulation Mechanics



Network Motifs: Evolution's Preferred Circuits

- Biological networks are complex and vast
- To understand their functionality in a *scalable* way one must choose the correct abstraction

“Patterns that occur in the real network significantly more often than in randomized networks are called network motifs”

Shai S. Shen-Orr et al., Network motifs in the transcriptional regulation network of Escherichia coli. Nature Genetics 31, 64 - 68 (2002)

- Moreover, these patterns are organised in non-trivial/non-random hierarchies

Radu Dobrin et al., Aggregation of topological motifs in the Escherichia coli transcriptional regulatory network. BMC Bioinformatics. 2004; 5: 10.

- ***Each network motif carries out a specific information-processing function***



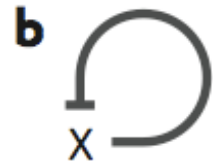
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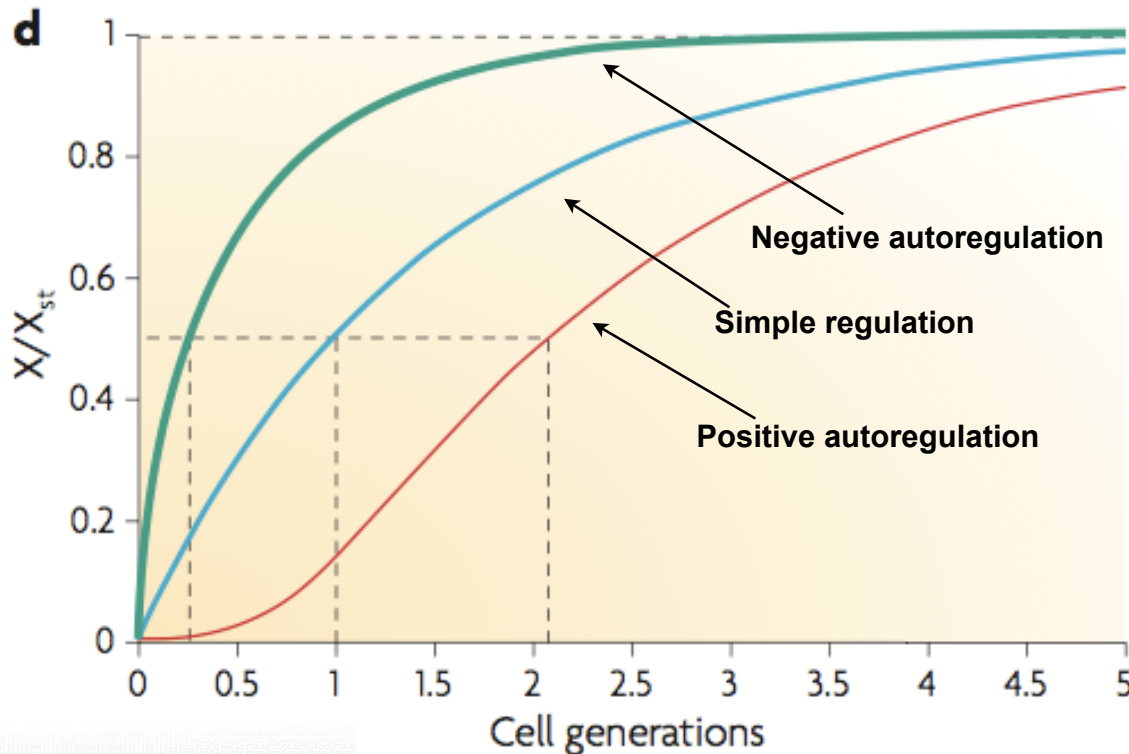
Y positively regulates X



Negative autoregulation



Positive autoregulation



$\rightarrow X$

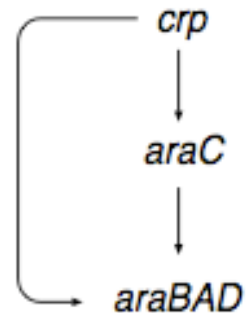
$$\frac{dx}{dt} = \beta - \alpha * x$$

$$x_{st} = \frac{\beta}{\alpha}$$

$$x(t) = x_{st} e^{-\alpha * t}$$

$$t_{\frac{1}{2}} = \frac{\log 2}{\alpha}$$

feedforward loop



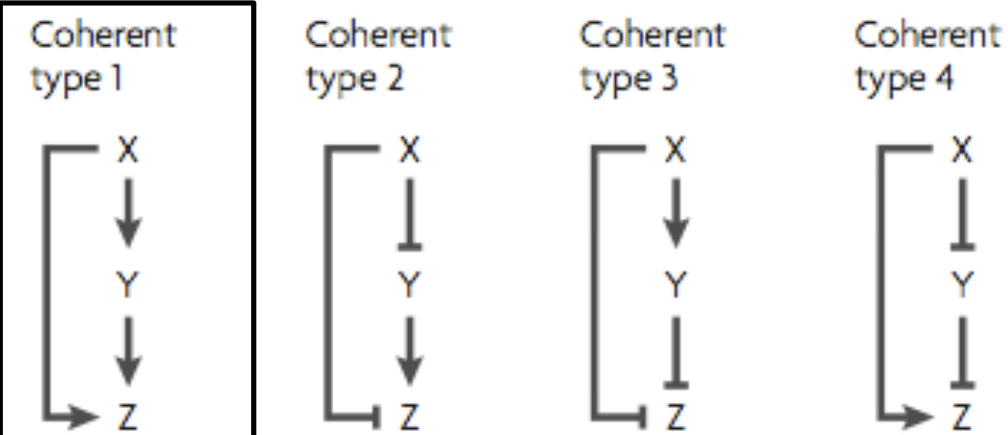
A general transcription factor regulating a second TF, called specific TF, such that both regulate effector operon Z.

In a coherent FFL, the direct effect of the general transcription factor (X) has the same sign (+/-) than the indirect net effect through Y in the effector operon.

If the arrow from X to Z has different sign than the internal ones then the loop is an incoherent FFL

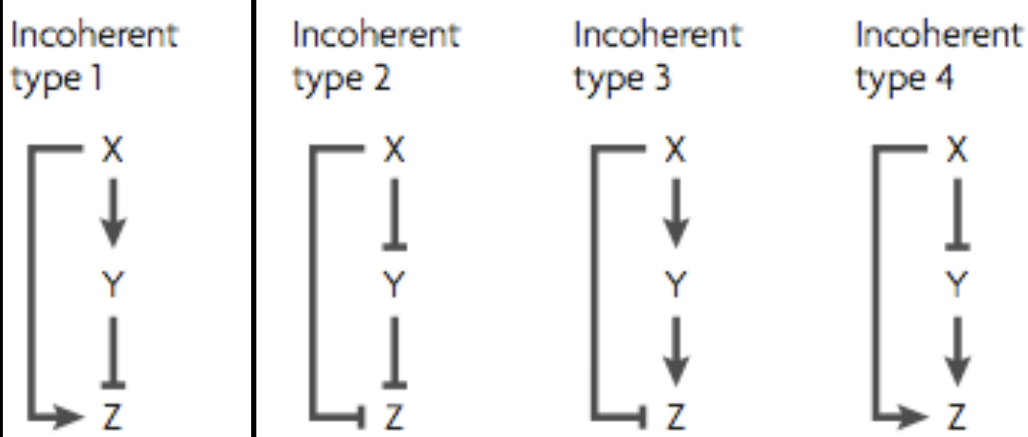
Shai S. Shen-Orr et al., Network motifs in the transcriptional regulation network of Escherichia coli. Nature Genetics 31, 64 - 68 (2002)

Coherent FFL



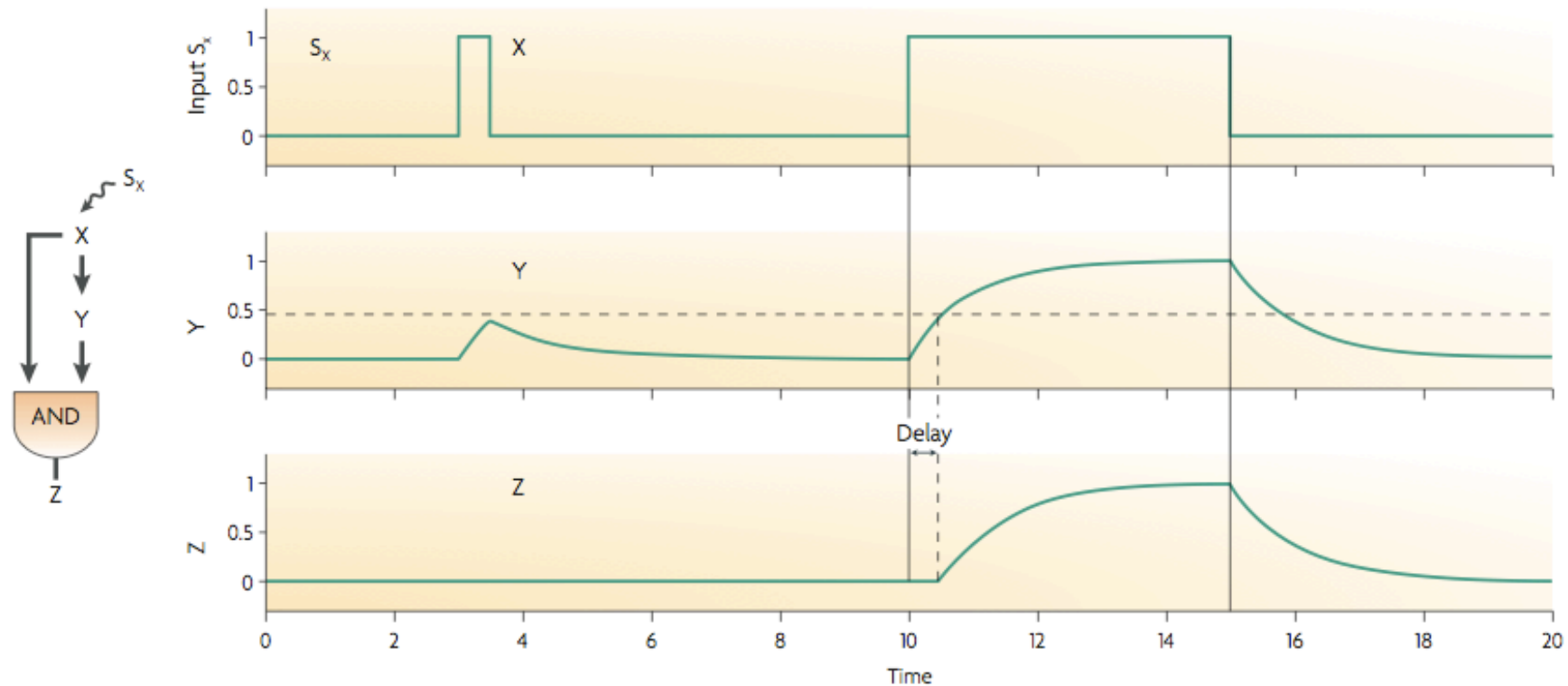
The C1-FFL is a 'sign-sensitive delay' element and a persistence detector.

Incoherent FFL



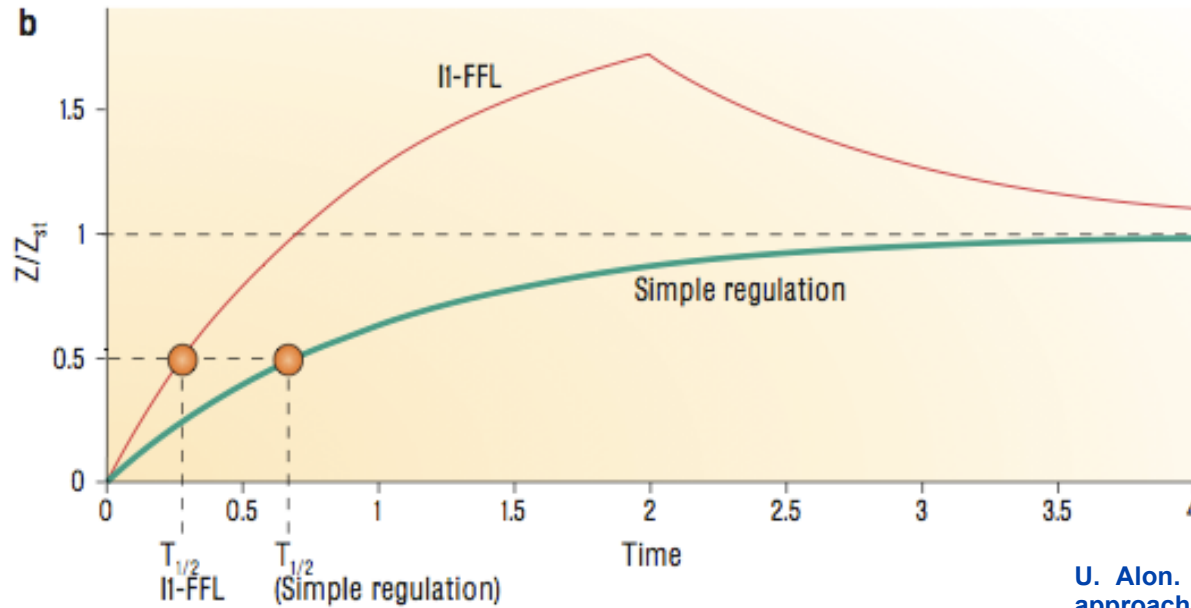
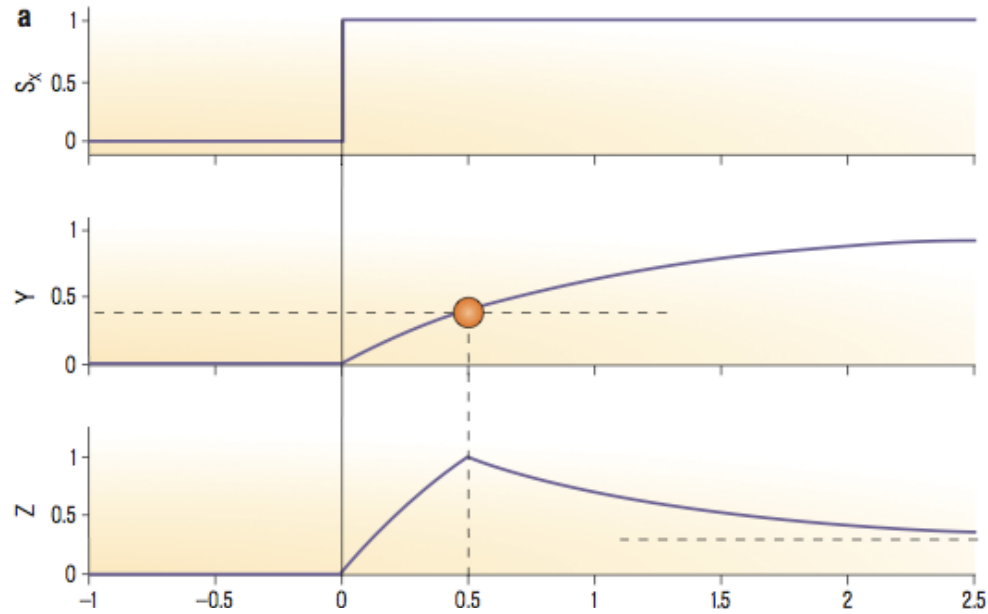
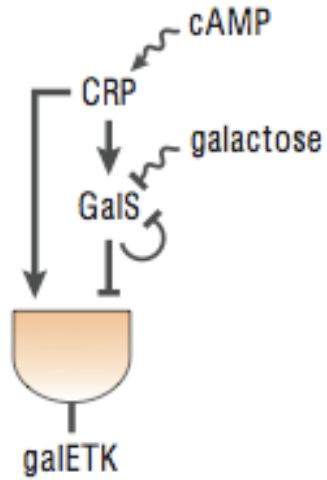
The I1-FFL is a pulse generator and response accelerator

most common
in E. Coli & S.
Cerevisiae



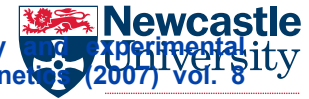
The C1-FFL is a ‘sign-sensitive delay’ element and a persistence detector.

If the integration function is “OR” (rather than “AND”), C1-FFL has no delay after stimulation by S_x but, instead, manifests the delay when the stimulation stops.



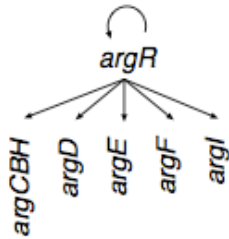
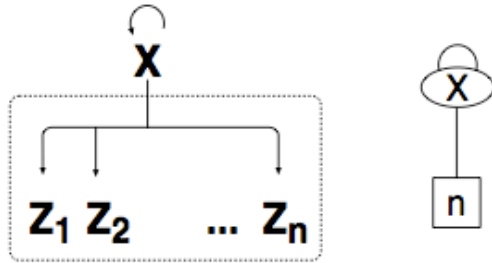
The I1-FFL is a pulse generator and response accelerator

U. Alon. Network motifs: theory and experimental approaches. Nature Reviews Genetics (2007) vol. 8 (6) pp. 450-461



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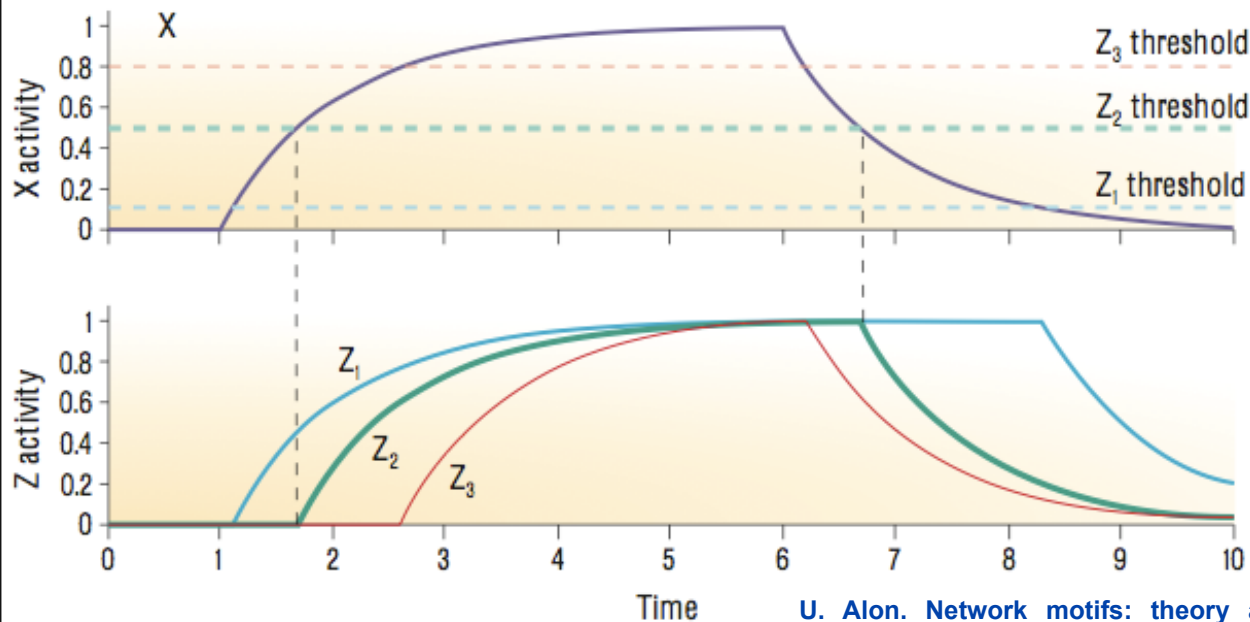
single input module (SIM)



SIM is defined by one TF controlling a set of operons, with the same signs and no additional control.

TFs in SIMs are mostly negative autoregulatory (70% in *E. coli*)

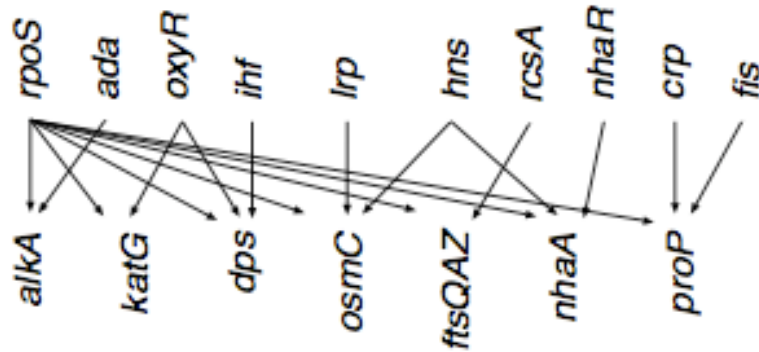
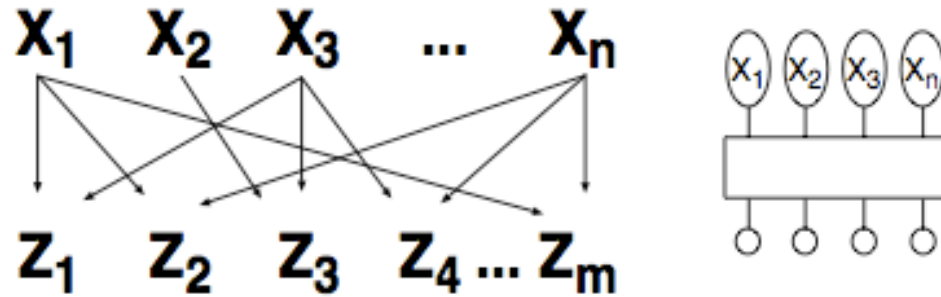
Shai S. Shen-Orr et al., Network motifs in the transcriptional regulation network of *Escherichia coli*. *Nature Genetics* 31, 64 - 68 (2002)



As the activity of the master regulator X changes in time, it crosses the different activation threshold of the genes in the SIM at different times, this prioritizing the activation of the operons

U. Alon. Network motifs: theory and experimental approaches. *Nature Reviews Genetics* (2007) vol. 8 (6) pp. 450-461
16/67

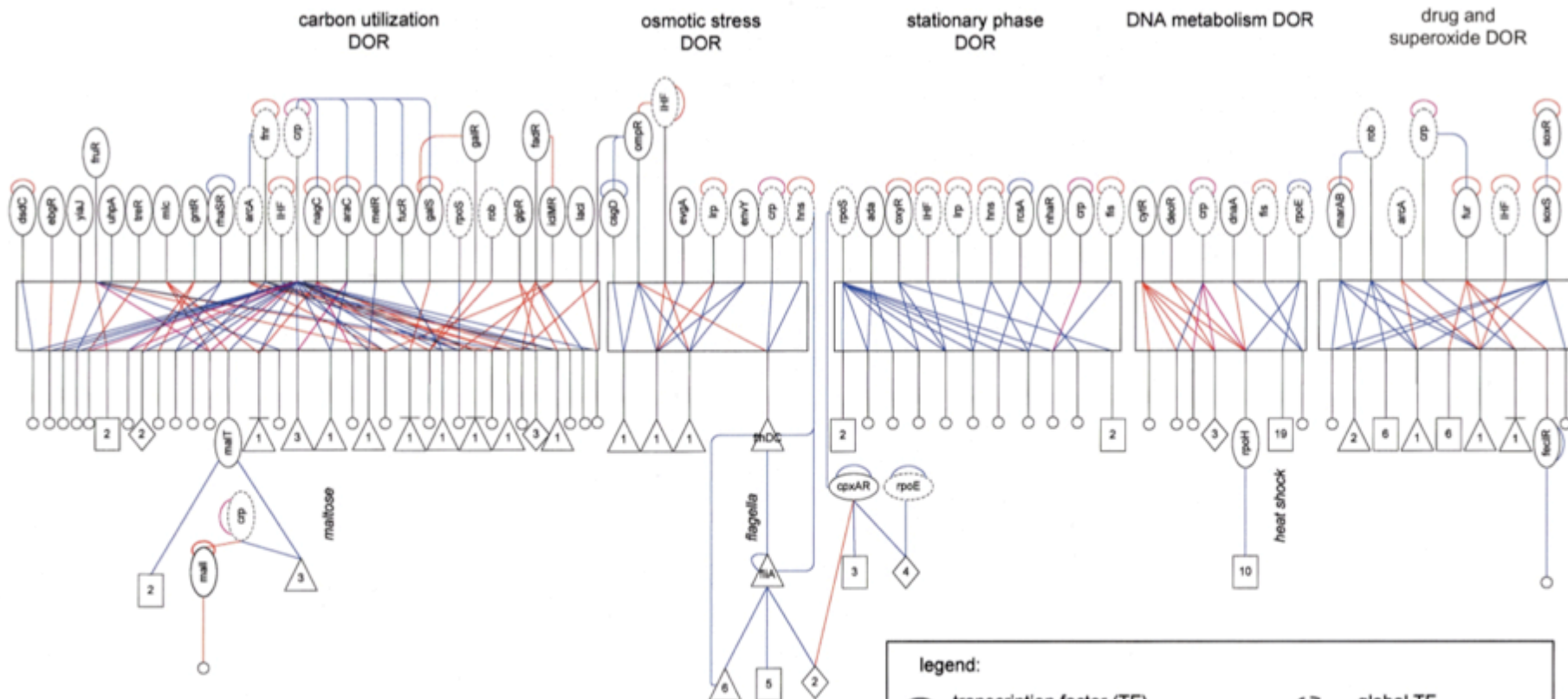
dense overlapping regulons (DOR)



DORs are layers of dense sets of TFs affecting multiple operons.

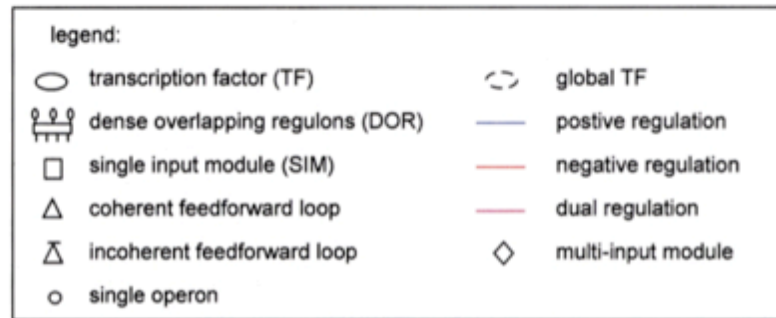
To understand the specific function of these “gate-arrays” one needs to know the input functions (AND/OR) for each output gene. This data is not currently available in most cases.

Shai S. Shen-Orr et al., Network motifs in the transcriptional regulation network of *Escherichia coli*. *Nature Genetics* 31, 64 - 68 (2002)



•The correct abstractions facilitates understanding in complex systems.

•Provide a route to engineering & programming cells.



Shai S. Shen-Orr et al., Network motifs in the transcriptional regulation network of Escherichia coli. *Nature Genetics* 9, 64 - 68 (2002)



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- The cell as a Computing Device for Biocomputing
- **P Systems for Representing Cellular Computation**
- Examples of Biocomputation
- Conclusions

P Systems

- Field of membrane computing initiated by Gheorghe Păun in 2000
- Inspired by the **hierarchical membrane structure** of eukaryotic cells
- **A formal language: precisely defined and machine processable**
- **An executable biology methodology**

Functional Entities

Container

- A boundary defining self/non-self (symmetry breaking).
- Maintain concentration gradients and avoid environmental damage.

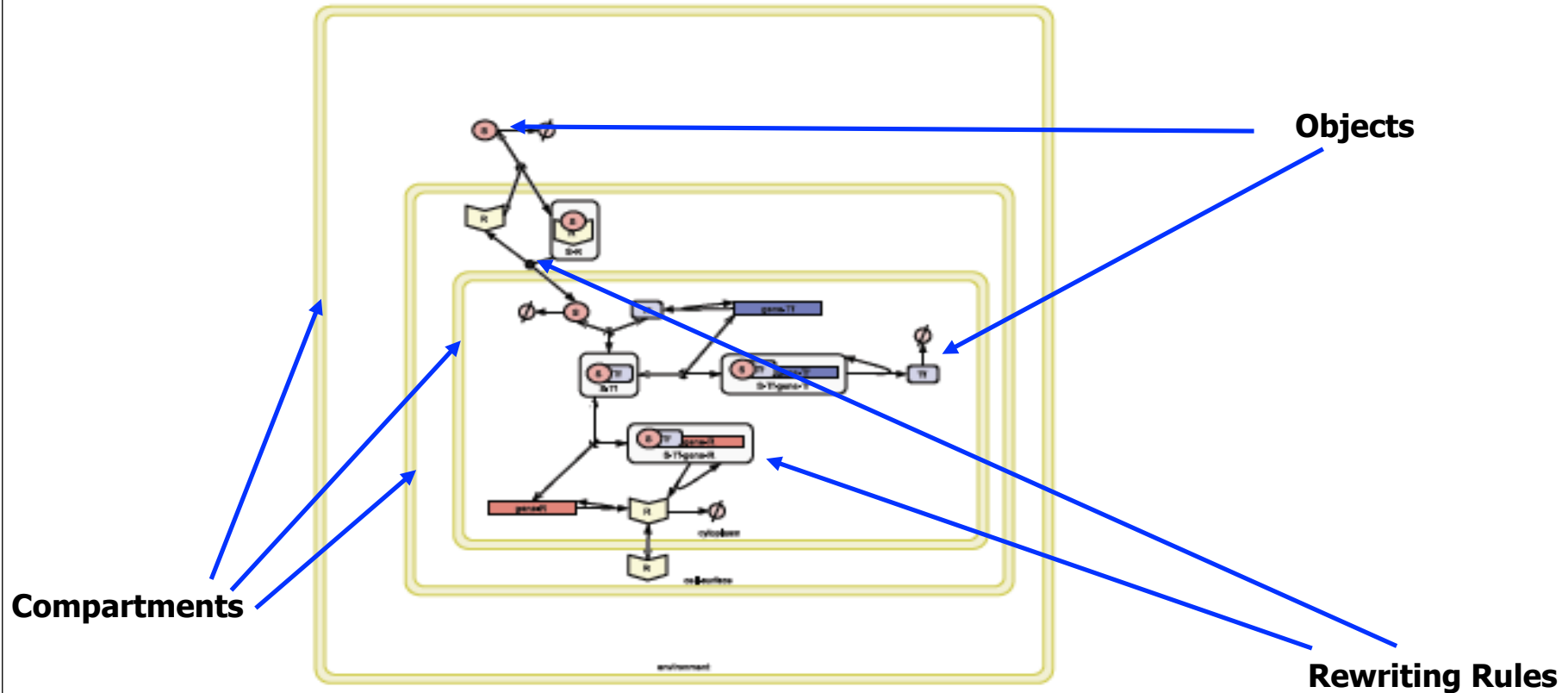
Metabolism

- Confining raw materials to be processed.
- Maintenance of internal structures (autopoiesis).

Information

- Sensing environmental signals / release of signals.
- Genetic information

Distributed and parallel rewriting systems in compartmentalised hierarchical structures.



Computational universality and efficiency.

Modelling Framework



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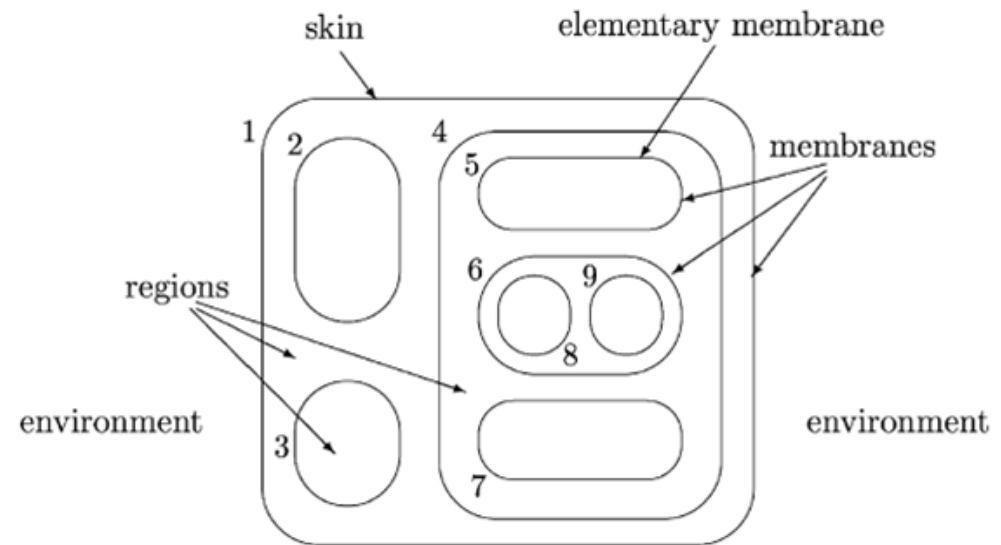
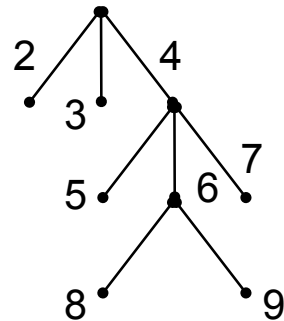


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Cell-like P systems

Intuitive Visual representation as a Venn diagram with a unique superset and without intersected sets.

formally equivalent to a tree:



the classic P system diagram appearing in most papers (Păun)

- a string of matching parentheses: $[_1 [_2]_2]_3]_3 [_4 [_5]_5]_6 [_8]_8]_9]_9]_6$

$[_7]_7]_4]_1$



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P-Systems: Modelling Principles

Molecules



Letters

Structured Molecules



Strings

Molecular Species



Multisets of letters/strings

Membranes /
organelles



Membrane

Biochemical activity



rules

Biochemical transport



Communication rules



Stochastic P Systems

$$\Pi = (O, L, \mu, M_1, M_2, \dots, M_n, R_{l_1}, \dots, R_{l_m})$$

- O is a finite alphabet representing **objects**;
- $L = \{l_1, \dots, l_m\}$ is a finite alphabet of **labels** identifying compartments types.
- μ is a **membrane structure** containing $n \geq 1$ membranes labelled with elements from L .
- $M_i = (l_i, w_i, s_i)$ is the **initial configuration** of membrane i with $l_i \in L$, $w_i \in O^*$ a finite multiset of objects and s_i a finite set of strings over O .
- $R_{l_t} = \{r_1^{l_t}, \dots, r_{k_t}^{l_t}\}$ is a finite set of **rewriting rules** associated with compartments of type $l_t \in L$.

Rewriting Rules

Rewriting rules on Multiset of OBJECTS

$$r_j^{lt} : \text{obj}_1 [\text{obj}_2]_l \xrightarrow{c_j^{lt}} \text{obj}'_1 [\text{obj}'_2]_l$$

with $\text{obj}_1, \text{obj}_2, \text{obj}'_1, \text{obj}'_2 \in O^*$ some finite multisets of objects and l a label from L . A multiset of objects, obj is represented as $\text{obj} = o_1 + o_2 + \dots + o_m$ with $o_1, \dots, o_m \in O$.

Rewriting rules on Multiset of STRINGS

$$r_j^{lt} : [\text{obj}_1 + \text{str}_1]_l \xrightarrow{c_j^{lt}} [\text{obj}'_1 + \text{str}'_1 + \dots + \text{str}'_p]_l$$

A string str is represented as $\text{str} = \langle s_1.s_2.\dots.s_i \rangle$ where $s_1, \dots, s_i \in O$.

A stochastic constant c_j^{lt} is associated specifically with each rule.

used by Multi-volume Gillespie's algorithm

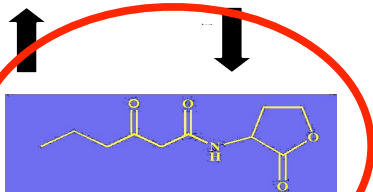
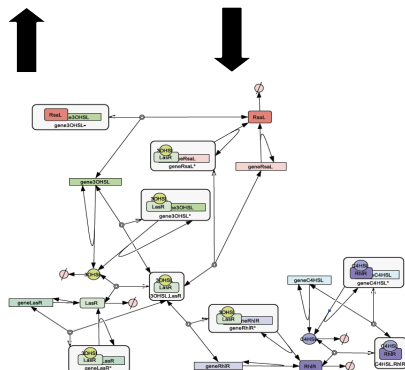
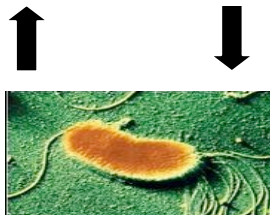
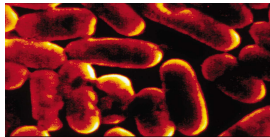


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Molecular Species

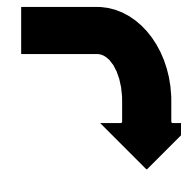
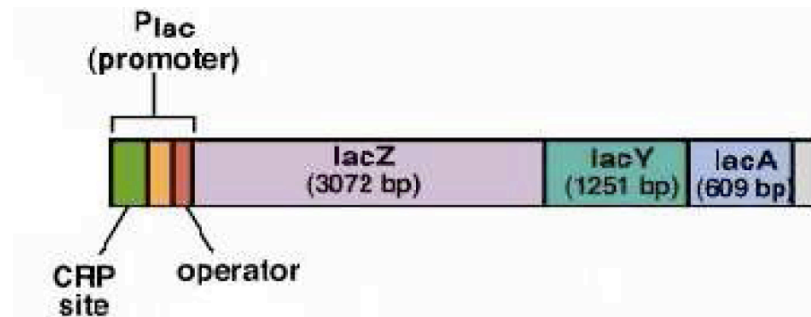


- A molecular species can be represented using **individual objects**.



LacI

- A molecular species with relevant internal structure can be represented **using a string**.

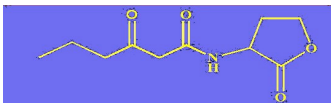
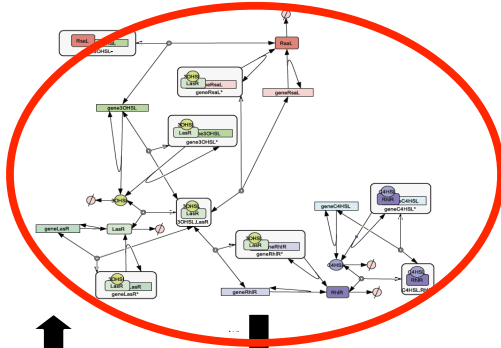
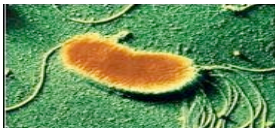
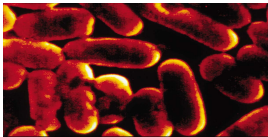


$\langle cap \times prom \times op \times lacZ_1 \dots lacZ_{30} \times lacY_1 \dots lacY_{12} \times lacA_1 \dots lacA_6 \rangle$

Molecular Interactions

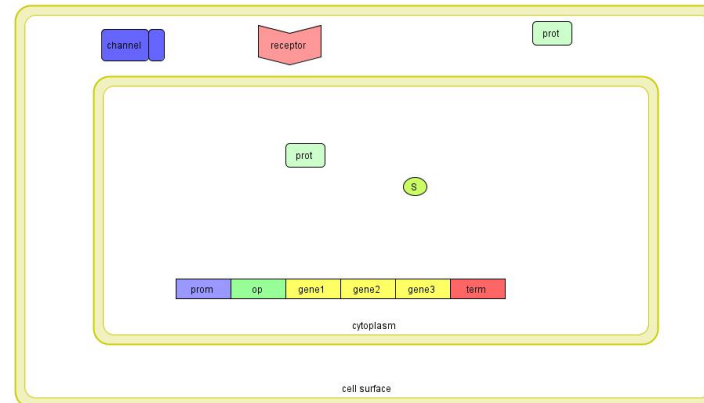
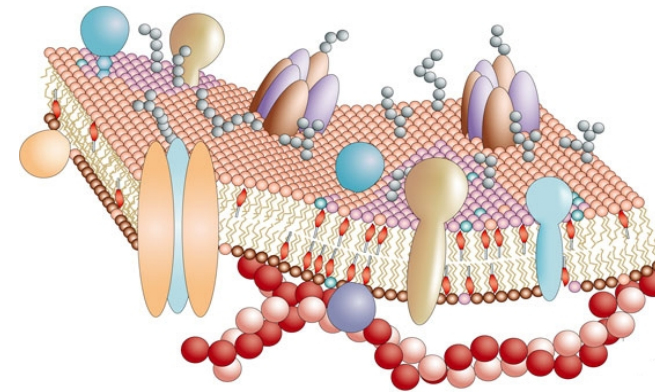
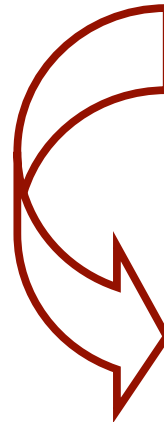
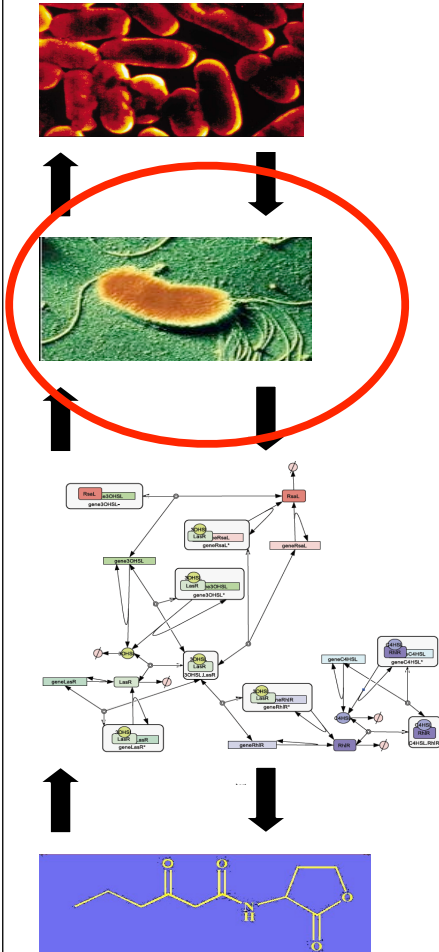
- Comprehensive and relevant rule-based schema for the most common molecular interactions taking place in living cells.

Transformation/Degradation
Complex Formation and Dissociation
Diffusion in / out
Binding and Debinding
Recruitment and Releasing
Transcription Factor Binding/Debinding
Transcription/Translation

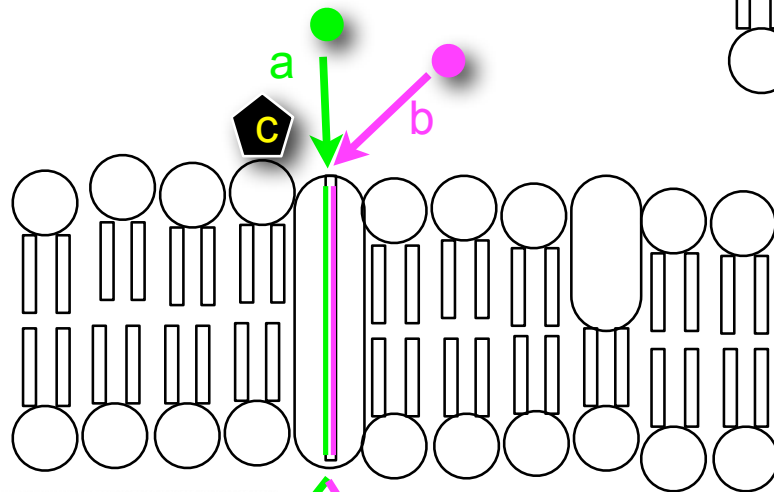
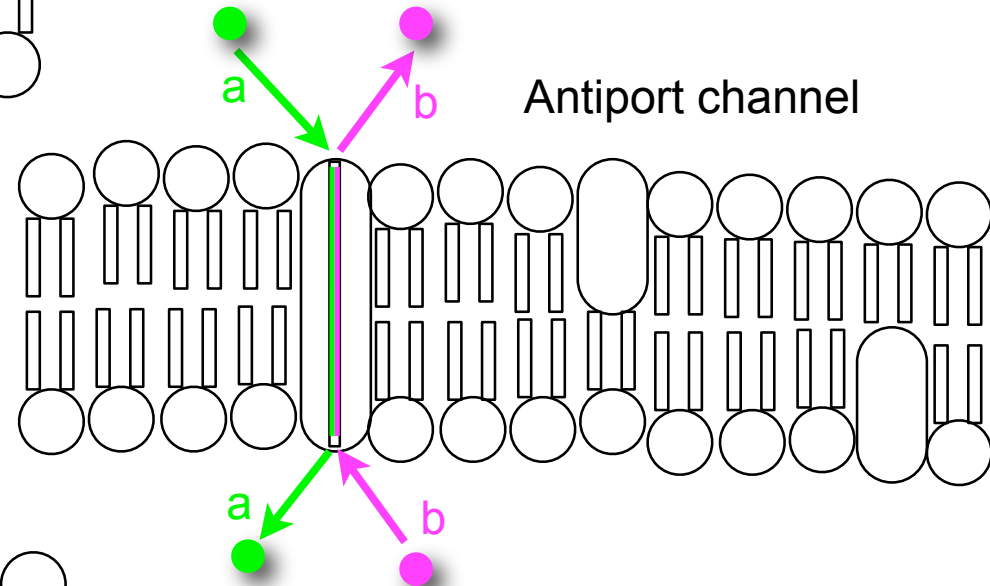
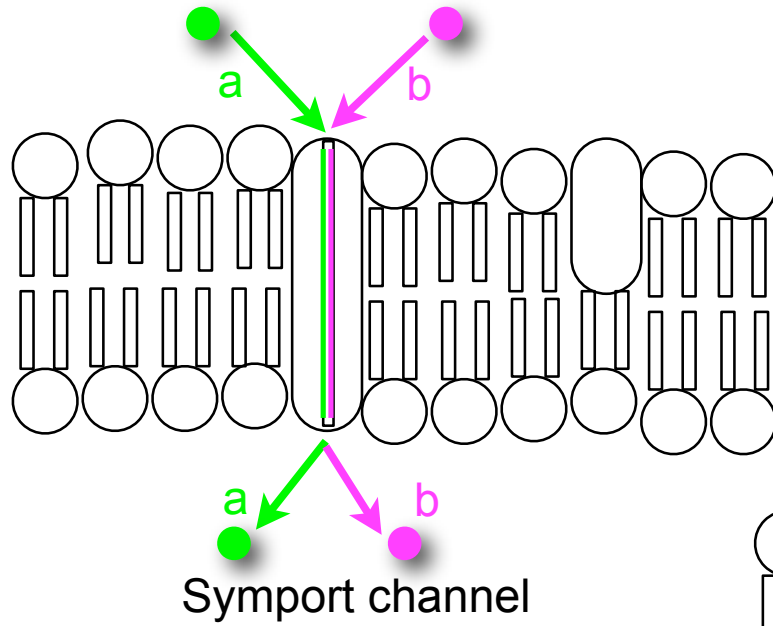


Compartments / Cells

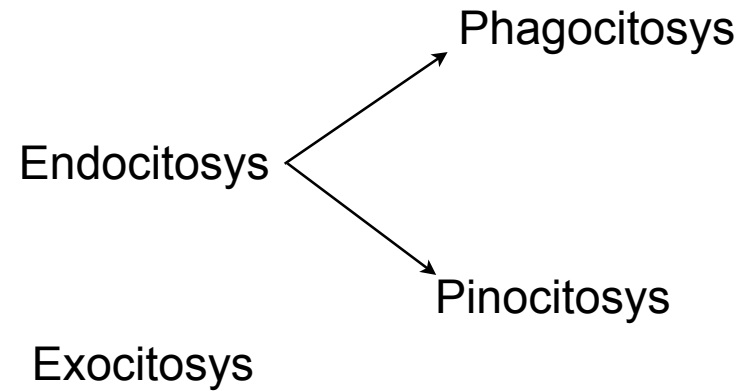
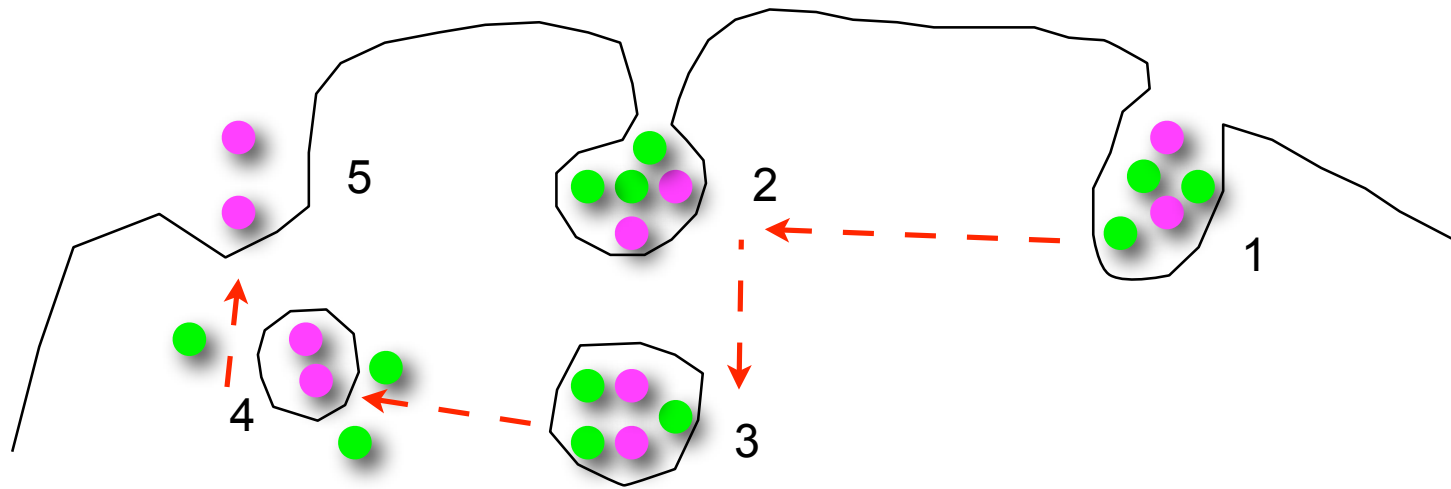
- **Compartments and regions are explicitly specified using membrane structures.**



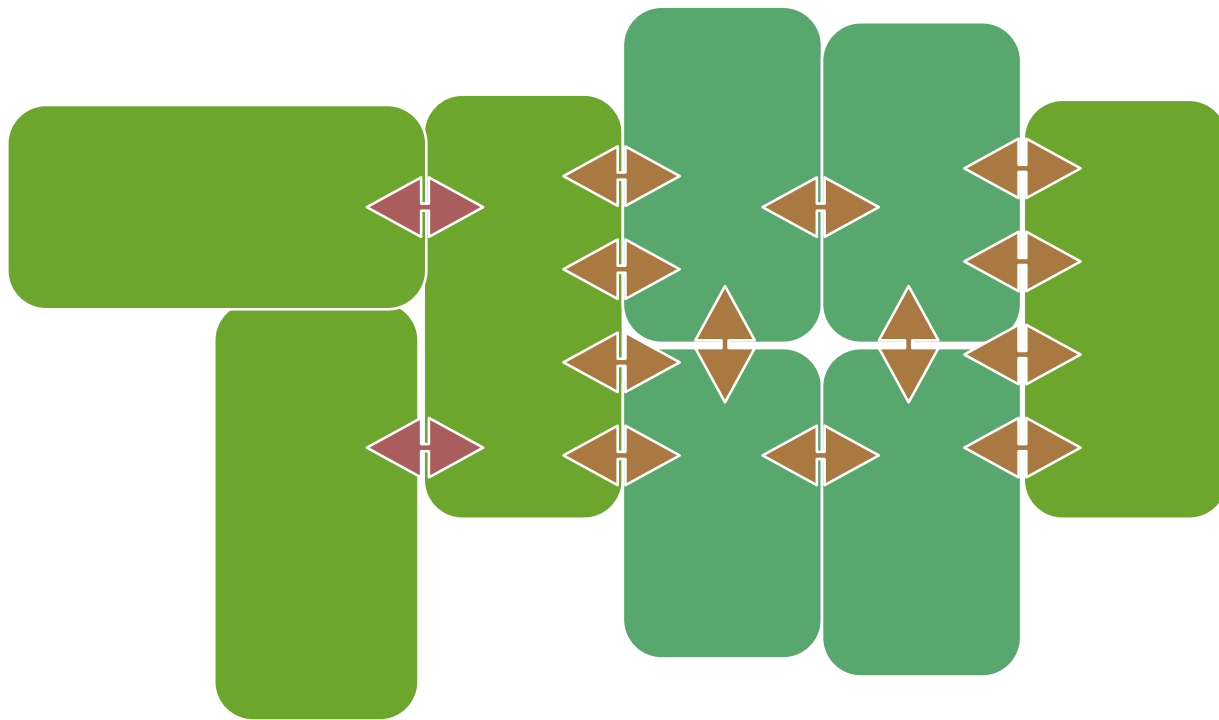
Transport Modalities



Transport Modalities

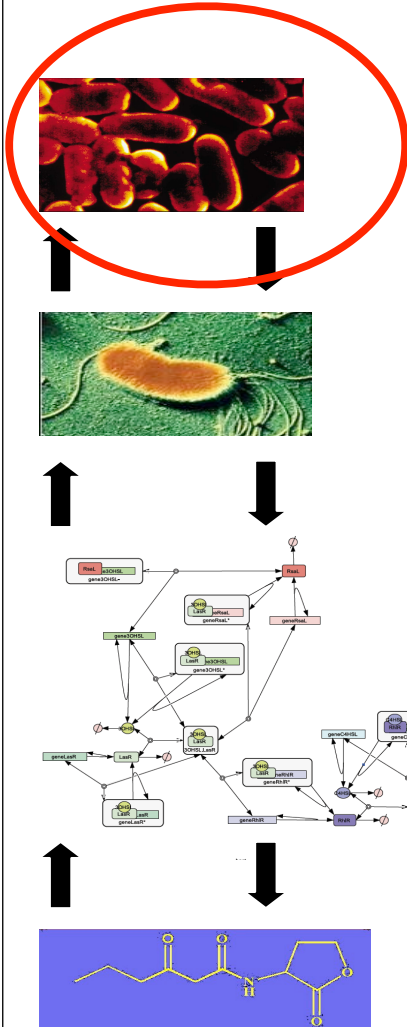


Transport Modalities



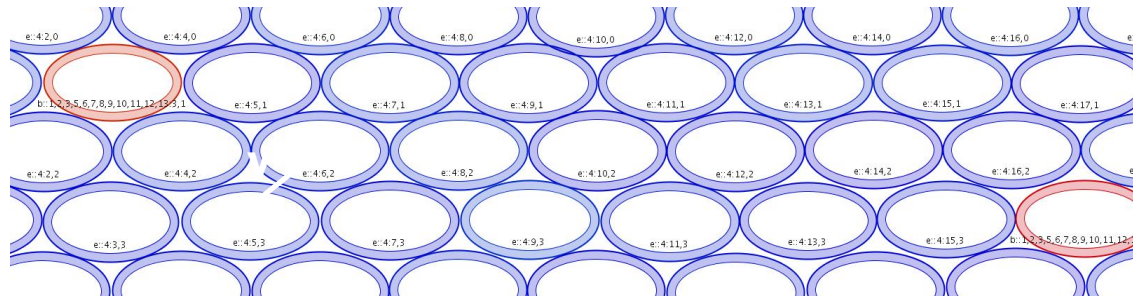
Highly specific:
cell specific & topology specific

Colonies / Tissues



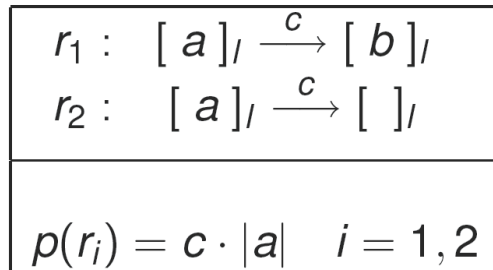
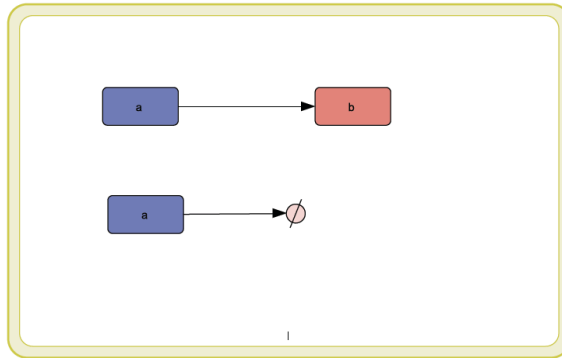
- Colonies and tissues are representing as **collection** of P systems distributed over a **lattice**.
- Objects can travel around the lattice through **translocation rules**.

$$[obj]_i \stackrel{v}{\Leftarrow} [] \xrightarrow{e_i^j} []_i \stackrel{v}{\Leftarrow} [obj]$$

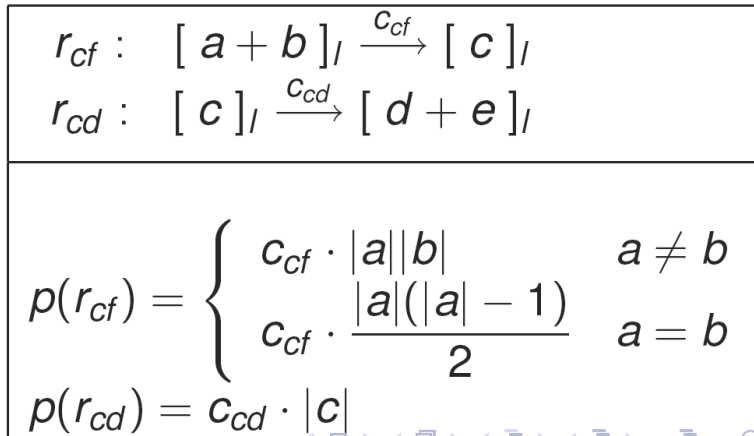
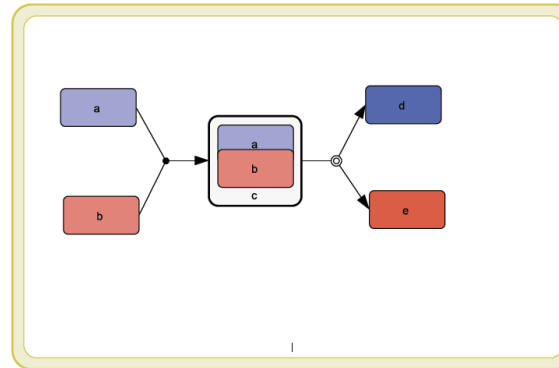


Molecular Interactions Inside Compartments

Transformation and degradation:

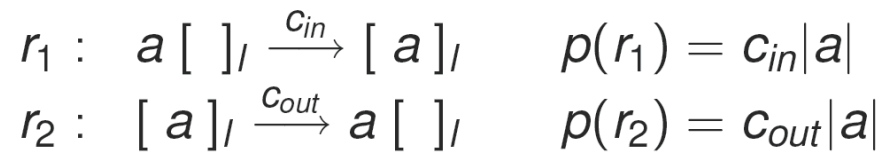
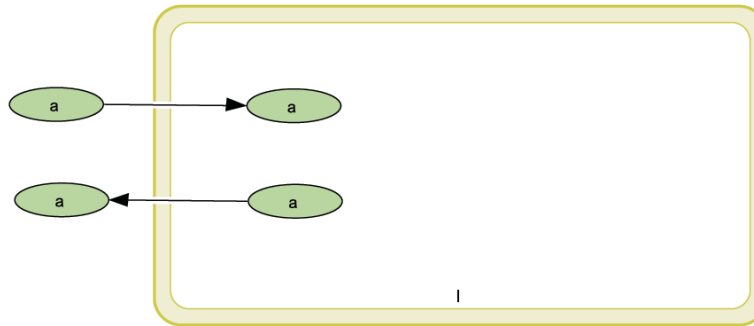


Complex formation and dissociation:



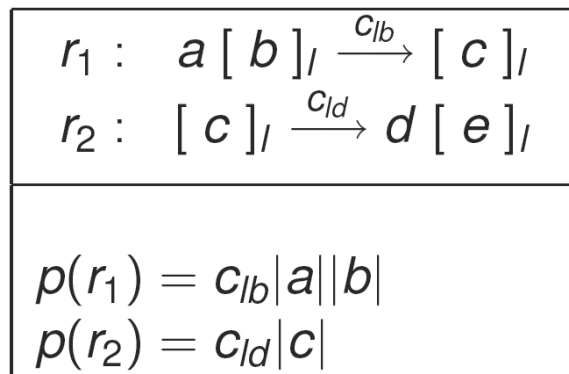
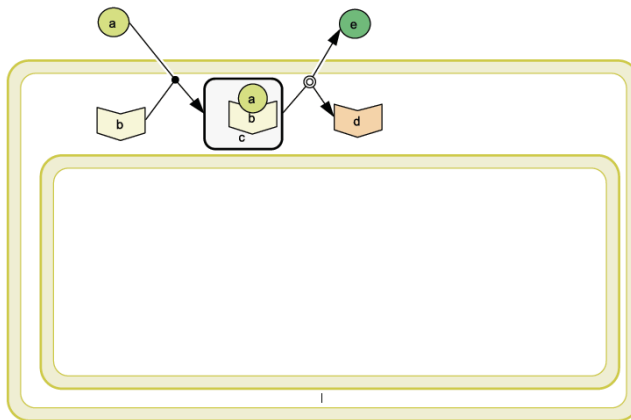
Passive Diffusion of Molecules

Diffusion in and out:

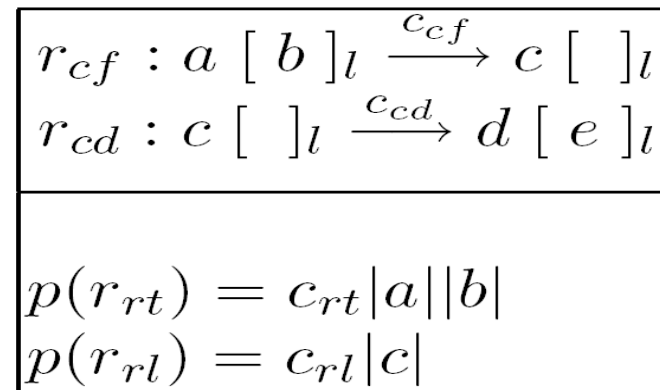
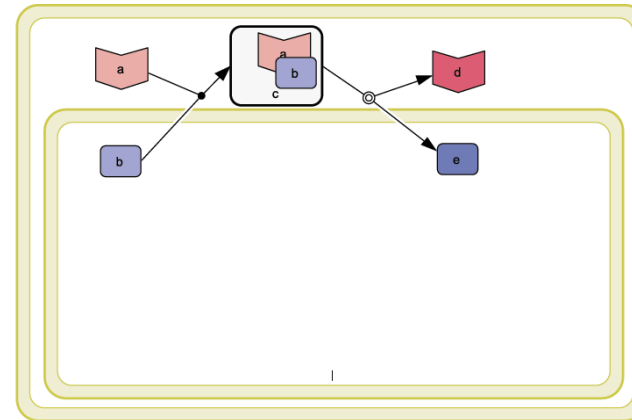


Signal Sensing and Active Transport

Binding and debinding:

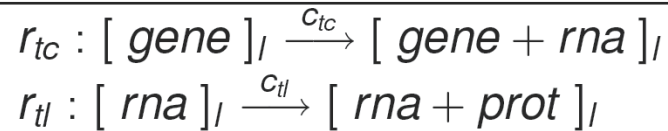
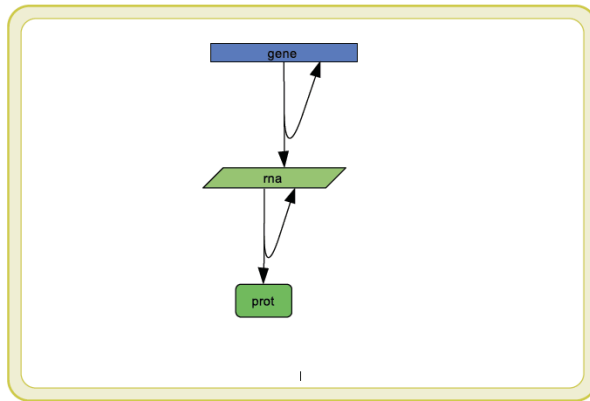


Recruitment and releasing:



Specification of Transcriptional Regulatory Networks

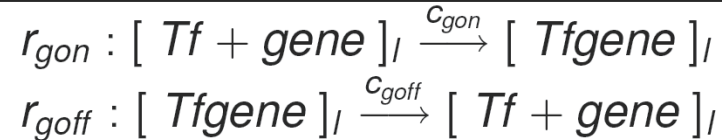
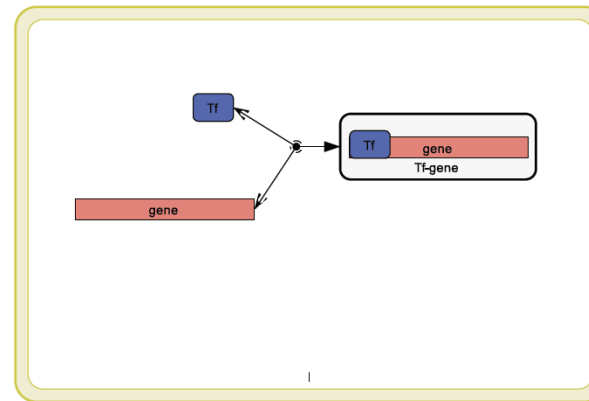
Transcription and Translation:



$$p(r_{tc}) = c_{tc} | gene |$$

$$p(r_{tl}) = c_{tl} | rna |$$

Transcription factor binding and debinding:

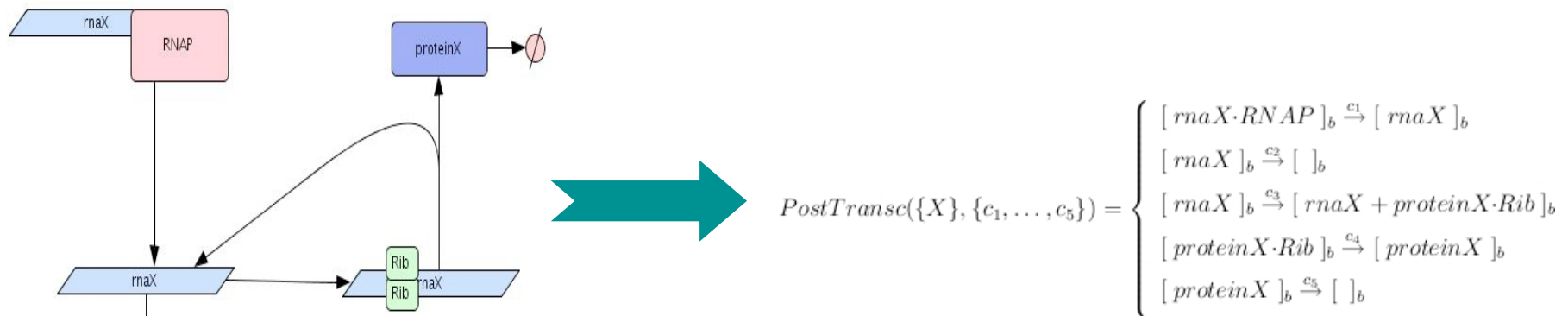


$$p(r_{gon}) = c_{gon} | Tf | | gene |$$

$$p(r_{goff}) = c_{goff} | Tfgene |$$

Post-Transcriptional Processes

- For each protein in the system, post-transcriptional processes like translational initiation, messenger and protein degradation, protein dimerisation, signal sensing, signal diffusion etc are represented using modules of rules.
- Modules can have also as parameters the stochastic kinetic constants associated with the corresponding rules in order to allow us to explore possible mutations in the promoters and ribosome binding sites in order to optimise the behaviour of the system.



Scalability through Modularity

Cellular functions arise from **orchestrated interactions between motifs** consisting of many molecular interacting species.

A ***P System model*** is a **set of rules** representing molecular interactions **motifs** that appear in many cellular systems.

F. J. Romero-Campero, J. Twycross, M. Camara, M. Bennett, M. Gheorghe, and N. Krasnogor. Modular assembly of cell systems biology models using p systems. *International Journal of Foundations of Computer Science*, 20(3):427-442, 2009.



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Basic P System Modules Used

Module Name	Type No	Module Size	Module	Biological Function
<i>Com</i>	3	1	$Com(\{X, Y, Z\}, \{c\}, \{l\}) = \{[X + Y]_l \xrightarrow{c} [Z]_l\}$	complex formation
<i>Diss</i>	4	1	$Diss(\{X, Y, Z\}, \{c\}, \{l\}) = \{[X]_l \xrightarrow{c} [Y + Z]_l\}$	complex dissociation
<i>UnReg</i>	0	4	$UnReg(\{G, R, P\}, \{c_1, c_2, c_3, c_4\}, \{l\}) =$ $= \left\{ \begin{array}{l} [G]_l \xrightarrow{c_1} [G + R]_l \\ [R]_l \xrightarrow{c_2} [R + P]_l \\ [R]_l \xrightarrow{c_3} [] \\ [P]_l \xrightarrow{c_4} []_l \end{array} \right\}$	unregulated expression
<i>Pos</i>	1	6	$Pos(\{Act, G, R, P\}, \{c_1, c_2, c_3, c_4, c_5, c_6\}, \{l\}) =$ $= \left\{ \begin{array}{l} [Act + G]_l \xrightarrow{c_1} [Act.G]_l \\ [Act.G]_l \xrightarrow{c_2} [Act + G]_l \\ [Act.G]_l \xrightarrow{c_3} [Act.G + R]_l \\ [R]_l \xrightarrow{c_4} [R + P]_l \\ [R]_l \xrightarrow{c_5} []_l \\ [P]_l \xrightarrow{c_6} []_l \end{array} \right\}$	positive regulated expression
<i>Neg</i>	2	2	$Neg(\{Rep, G\}, \{c_1, c_2\}, \{l\}) =$ $= \left\{ \begin{array}{l} [Rep + G]_l \xrightarrow{c_1} [Rep.G]_l \\ [Rep.G]_l \xrightarrow{c_2} [Rep + G]_l \end{array} \right\}$	negative regulated expression

Characterisation/Encapsulation of Cellular Parts: Gene Promoters

□ A modeling language for the design of synthetic bacterial colonies.

□ A *module*, set of rules describing the molecular interactions involving a cellular part, provides **encapsulation and abstraction**.

□ Collection or **libraries of reusable cellular parts and reusable models**.



PluxOR1({X},{c1, c2, c3, c4, c5, c6, c7, c8, c9},{1}) = {

type: promoter

sequence: ACCTGTAGGATCGTACAGGTTTACGCAAGAAATGGTTTGTATAGTCGAAATACCTCTGGCGGTGATA

rules:

r1(c1): [LuxR2 + PluxPR.X] => [PluxPR.LuxR2.X]

r2(c2): [PluxPR.LuxR2.X] => [LuxR2 + PluxPR.X]

...
r5(c5): [CI2 + PluxPR.X] => [PluxPR.CI2.X]

r6(c6): [PluxPR.CI2.X] => [CI2 + PluxPR.X]

...
r9(c9): [PluxPR.LuxR2.X] => [PluxPR.LuxR2.X + RNAP.X]

E. Davidson (2006) *The Regulatory Genome, Gene Regulation Networks in Development and Evolution*, Elsevier



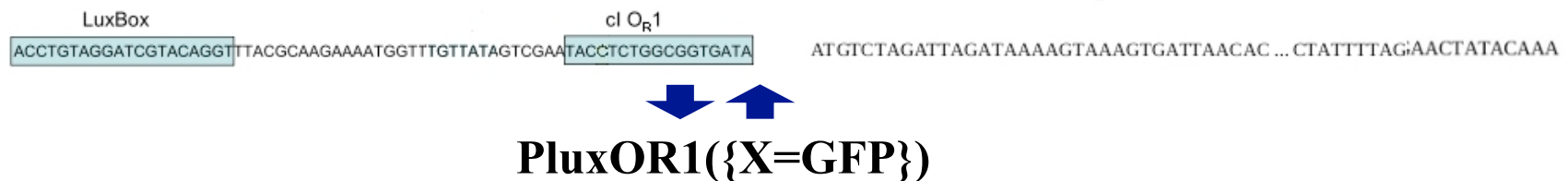
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Module Variables: Recombinant DNA, Directed Evolution, Chassis selection

- ❑ **Recombinant DNA:** Objects variables can be instantiated with the name of specific genes.



- ❑ **Directed evolution:** Variables for stochastic constants can be instantiated with specific values.

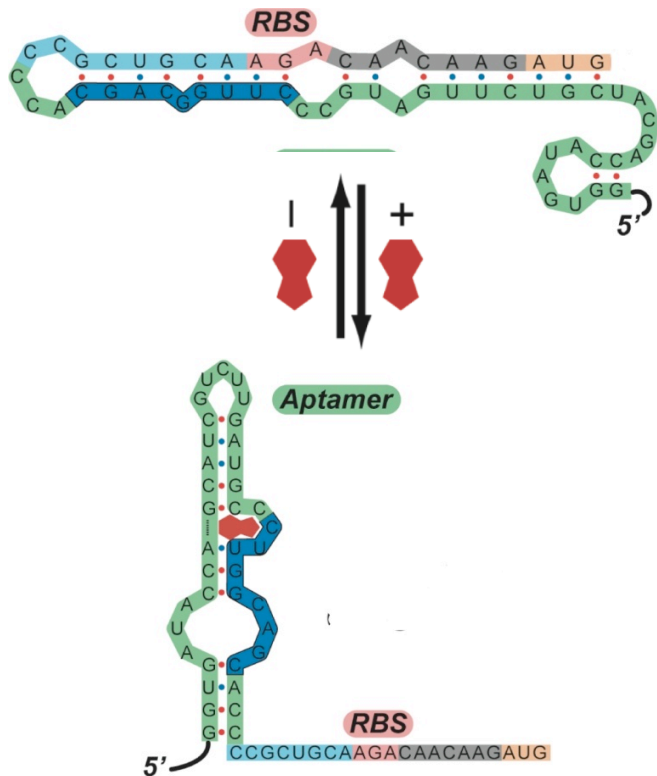


- ❑ **Chassis Selection:** The variable for the label can be instantiated with the name of a chassis.

PluxOR1({X=GFP},{...,c4=10,...},{l=DH5α })

Characterisation/Encapsulation of Cellular Parts: Riboswitches

□ A **riboswitch** is a piece of RNA that *folds* in different ways depending on the presence or absence of specific molecules regulating translation.



$\text{ToppRibo}(\{X\}, \{c1, c2, c3, c4, c5, c6\}, \{1\}) = \{$

type: riboswitch

sequence:GGTGATACCAGCATCGTCTTGATGCCCTTGG
CAGCACCCCGCTGCAAGACAACAAGATG

rules:

- r1(c1): [RNAP.ToppRibo.X] => [ToppRibo.X]
- r2(c2): [ToppRibo.X] => []
- r3(c3): [ToppRibo.X + theop] => [ToppRibo*.X]
- r4(c4): [ToppRibo*.X] => [ToppRibo.X + theop]
- r5(c5): [ToppRibo*.X] => []
- r6(c6): [ToppRibo*.X] => [ToppRibo*.X + Rib.X]

}

Characterisation/Encapsulation of Cellular Parts: Degradation Tags

□ **Degradation tags** are amino acid sequences recognised by proteases. Once the corresponding DNA sequence is fused to a gene the half life of the protein is reduced considerably.



degLVA({X},{c1, c2},{l}) = {

type: degradation tag

sequence: CAGCAAACGACGAAAACACTACGCTTTAGTAGCT

rules:

r1(c1): [Rib.X.degLVA] => [X.degLVA]

r2(c2): [X.degLVA] => []

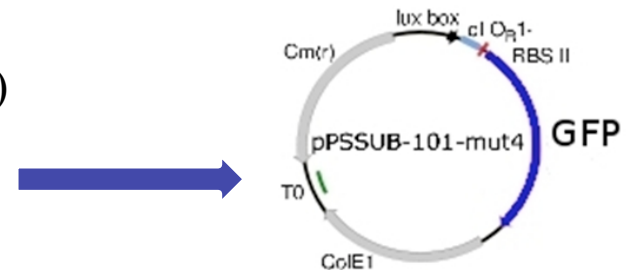
}

Higher Order Modules: Building Synthetic Gene Circuits



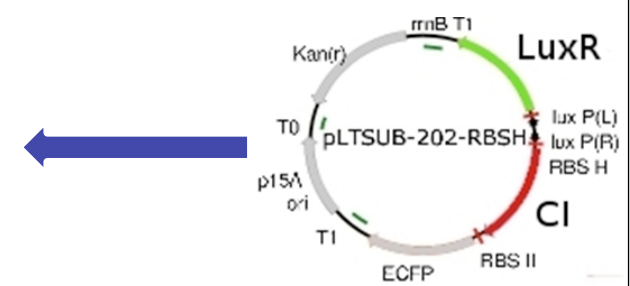
```

3OC6_repressible_sensor({X}) = {
  PluxOR1({X=ToppRibo.geneX.degLVA}, {...}, {l=DH5α})
  ToppRibo({X=geneX.degLVA}, {...}, {l=DH5α})
  degLVA({X}, {...}, {l=DH5α})
}
    
```



```

Plux({X=ToppRibo.geneCI.degLVA}, {...}, {l=DH5α})
ToppRibo({X=geneCI.degLVA}, {...}, {l=DH5α})
degLVA({CI}, {...}, {l=DH5α})
    
```



```

PtetR({X=ToppRibo.geneLuxR.degLVA}, {...}, {l=DH5α})
Weiss_RBS({X=LuxR}, {...}, {l=DH5α})
Deg({X=LuxR}, {...}, {l=DH5α})
    
```



Stochastic P Systems Are *Executable* Programs

The virtual machine running these programs is a “**Gillespie Algorithm (SSA)**”. It generates trajectories of a stochastic system:

A stochastic constant is associated with each rule.

A propensity is computed for each rule by multiplying the stochastic constant by the number of distinct possible combinations of the elements on the left hand side of the rule.

F. J. Romero-Campero, J. Twycross, M. Camara, M. Bennett, M. Gheorghe, and N. Krasnogor.
Modular assembly of cell systems biology models using p systems. *International Journal of Foundations of Computer Science*, 2009

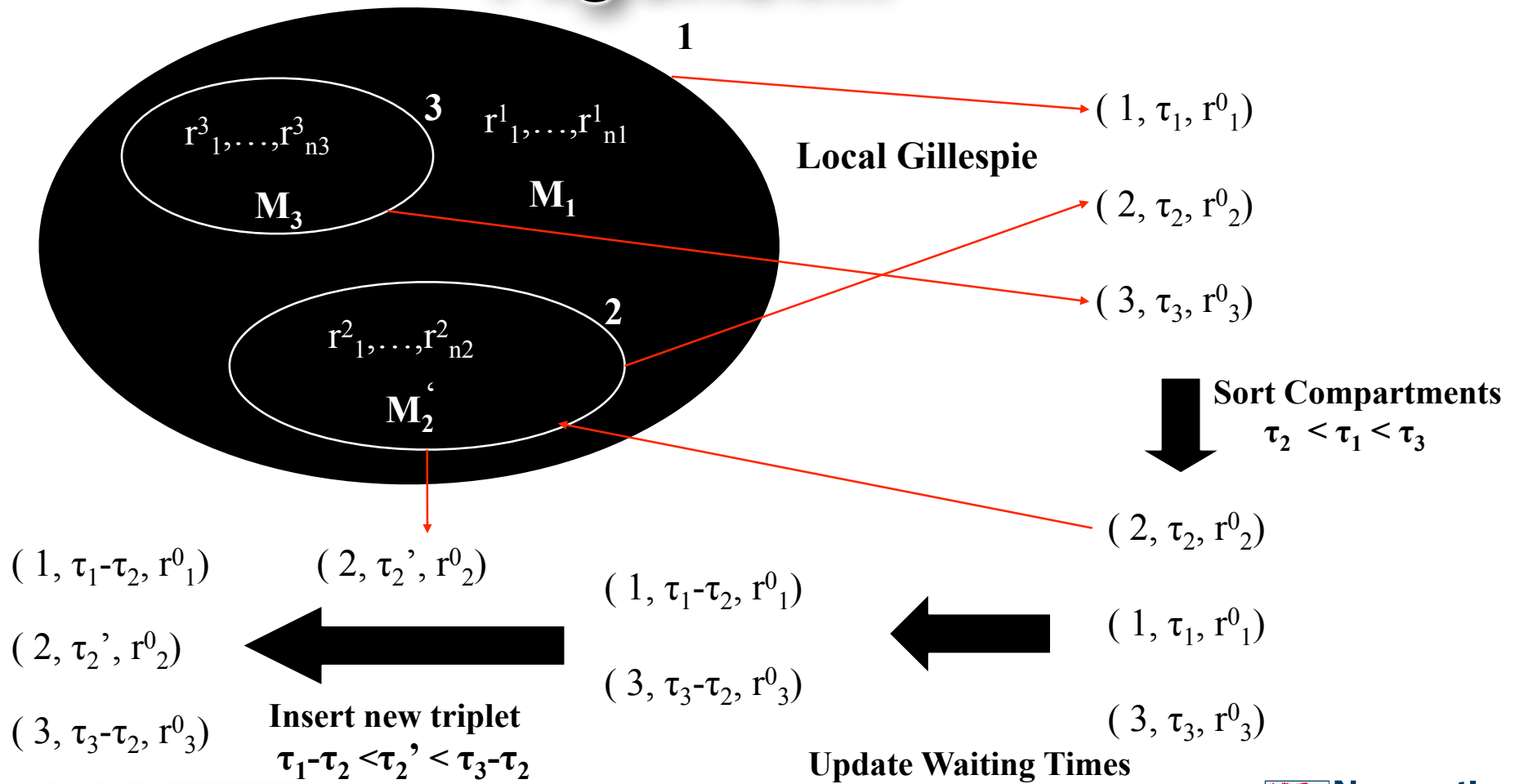


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Multicompartmental Gillespie Algorithm



Outline

- The cell as a Computing Device for Biocomputing
- P Systems for Representing Cellular Computation
- Examples of Biocomputation
- Conclusions

An example: A Pulse Generator

- **Two different bacterial strains** carrying specific synthetic gene regulatory networks are used.
- The first strain produces a diffusible **signal AHL**.
- The second strain possesses a *synthetic gene regulatory* network which produces a **pulse of GFP** after AHL sensing within a range of values (Band Pass).

S. Basu, R. Mehreja, et al. (2004) Spatiotemporal control of gene expression with pulse generating networks, PNAS, 101, 6355-6360

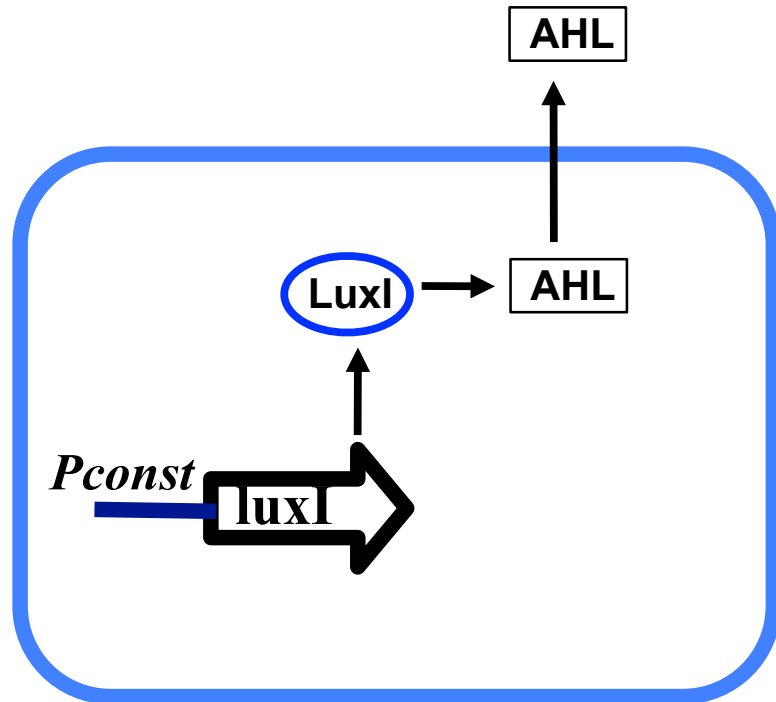


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Sender Cells



SenderCell()=

{

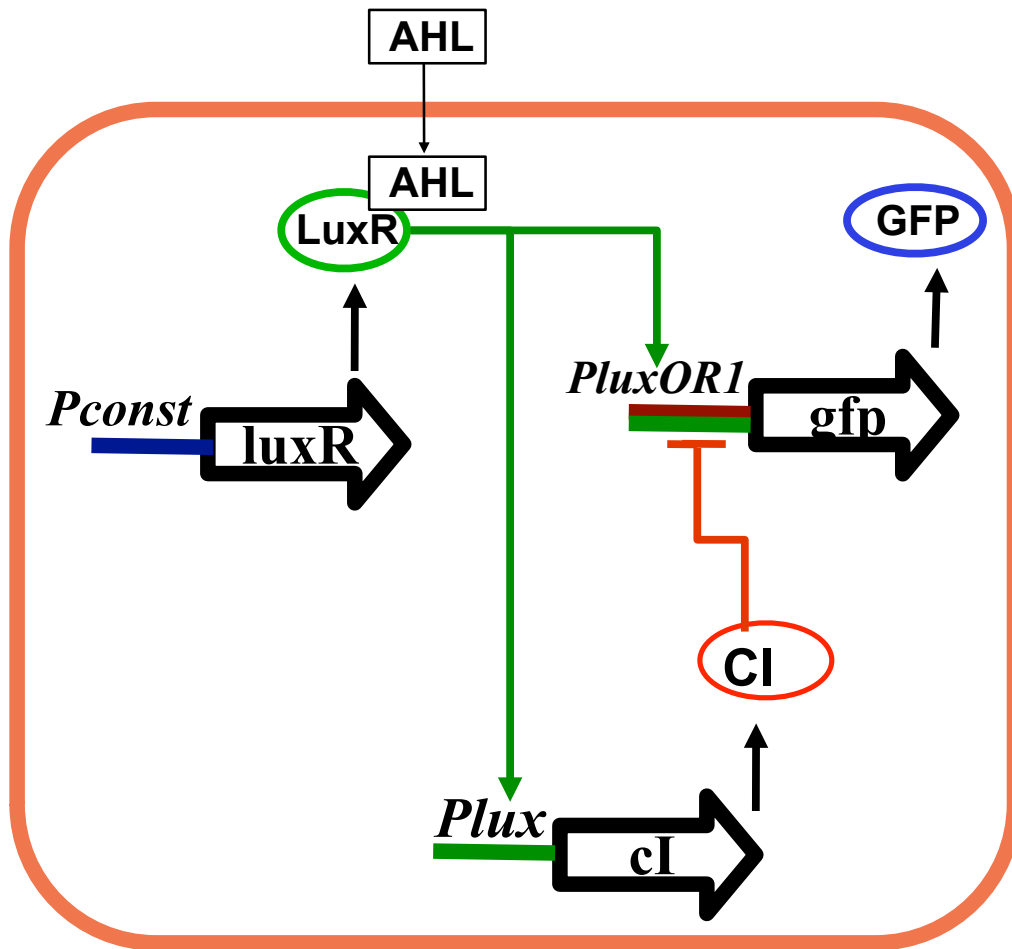
Pconst({X = luxI } , ...)

PostTransc({X=LuxI} , {c₁=3.2, ...})

Diff({X=AHL} , {c=0.1})

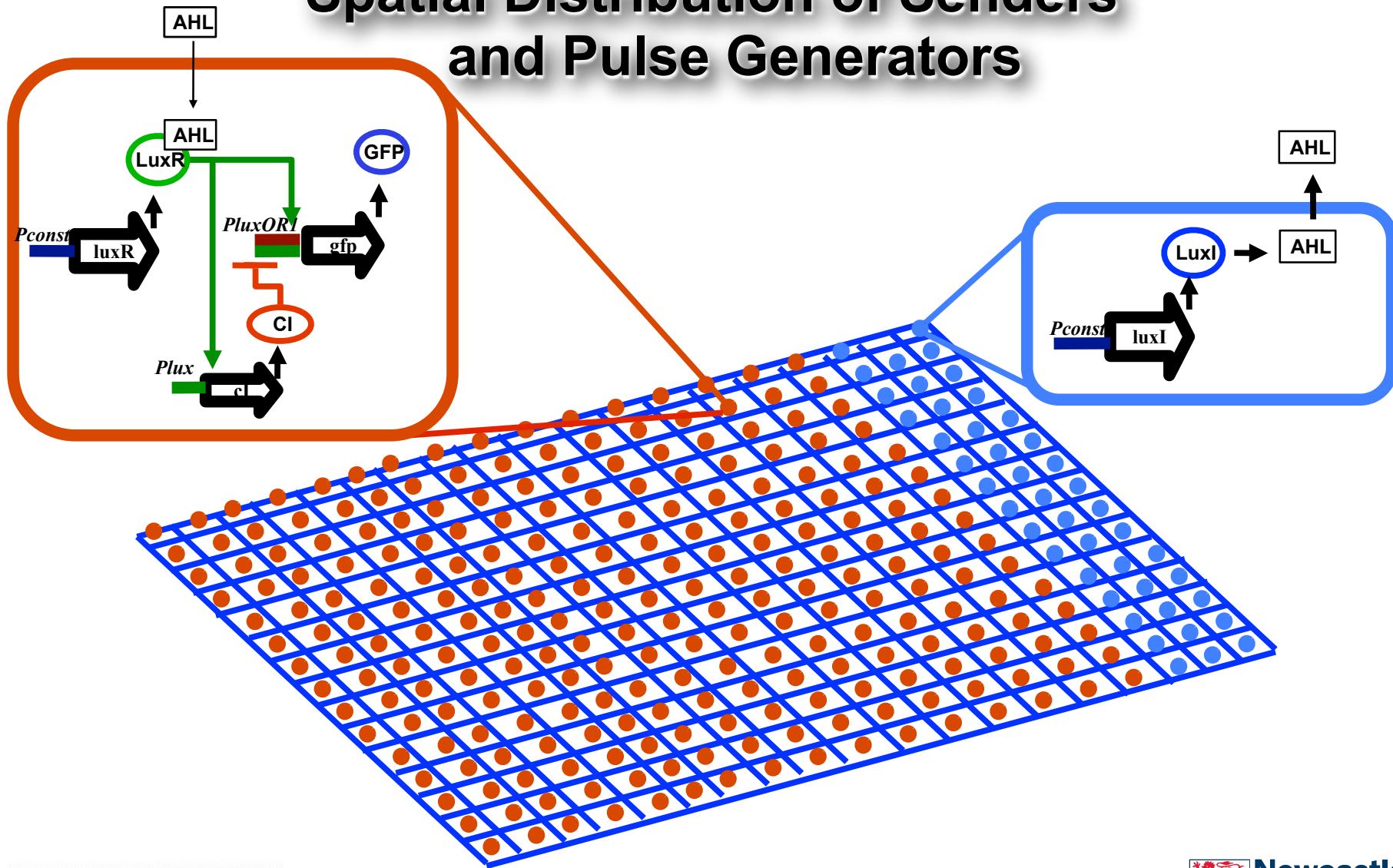
}

Pulse Generating Cells



PulseGenerator()=
 {
 Pconst({X=luxR},...)
 PluxOR1({X=gfp},...)
 Plux({X=cI},...)
 ...
 ...
 Diff({X=AHL},...)
 }

Spatial Distribution of Senders and Pulse Generators



Pulse propagation - simulation I

Simulation I

PulseGenerator2.htm

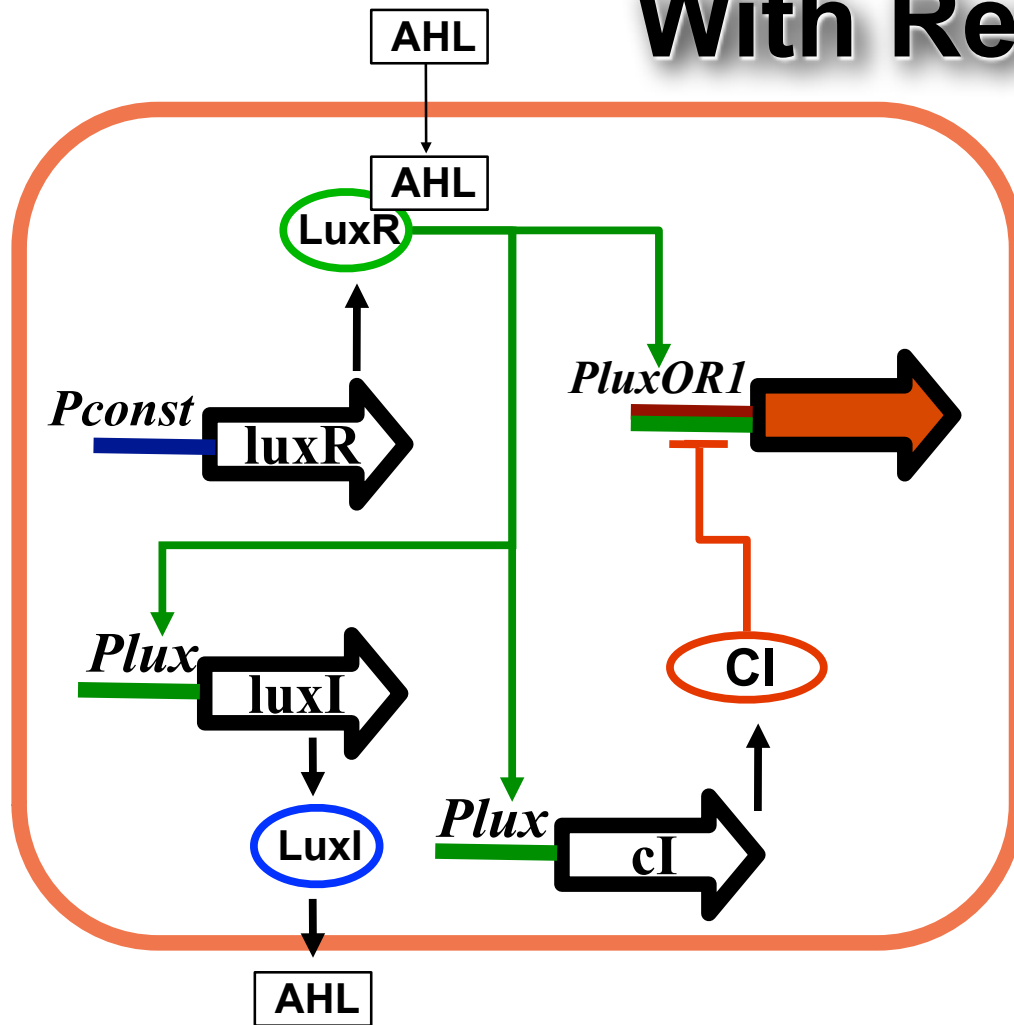


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Pulse Generating Cells With Relay



PulseGenerator(**X**) =

{

Pconst({X=luxR},...)

PluxOR1({**X**},...),

Plux({X=cI},...),

...

Diff({X=AHL},...),

Plux({X=luxI},...)

}

Pulse propagation & Rely-simulation II

Simulation II

PulseGenerator3.htm

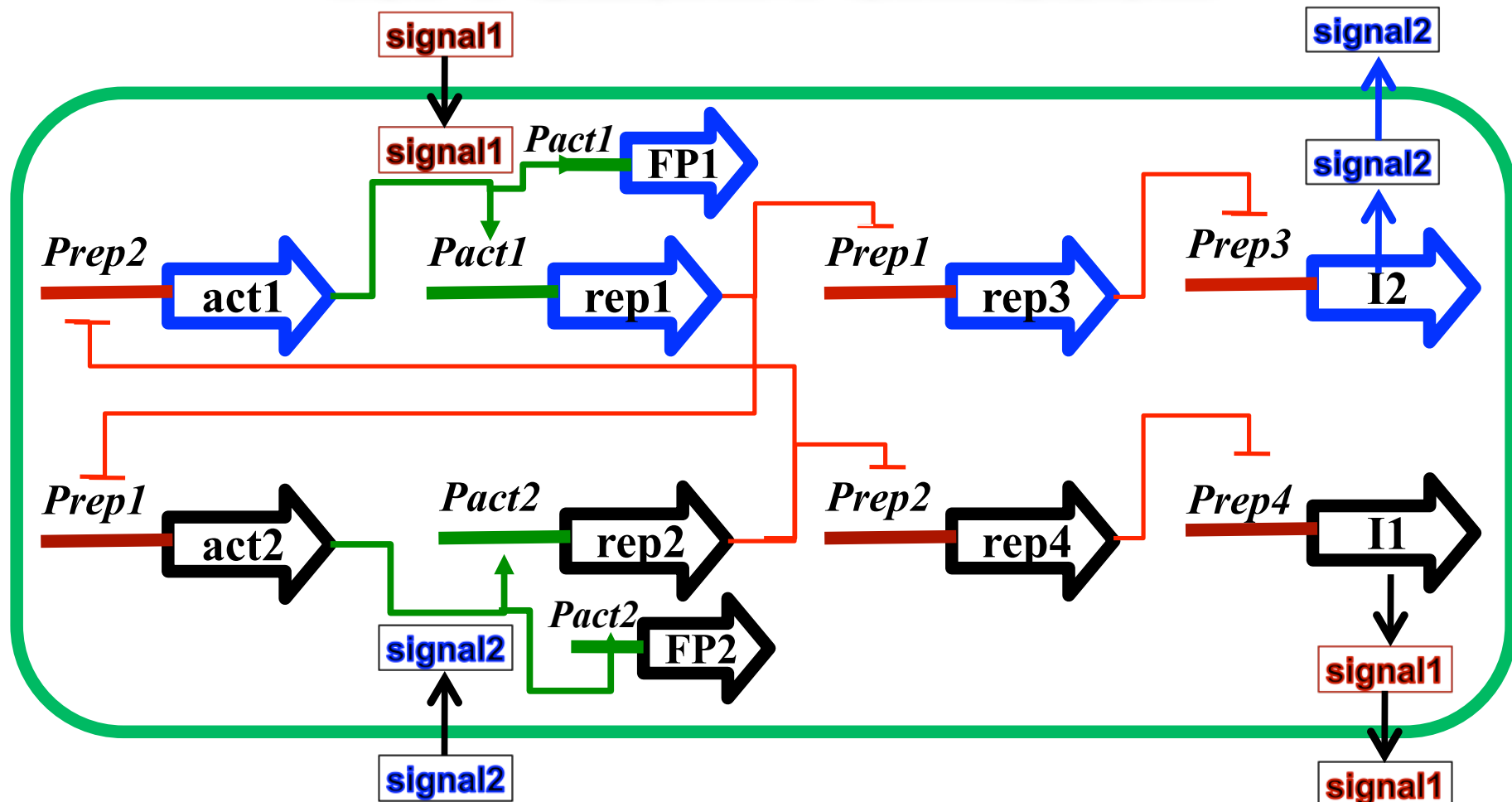


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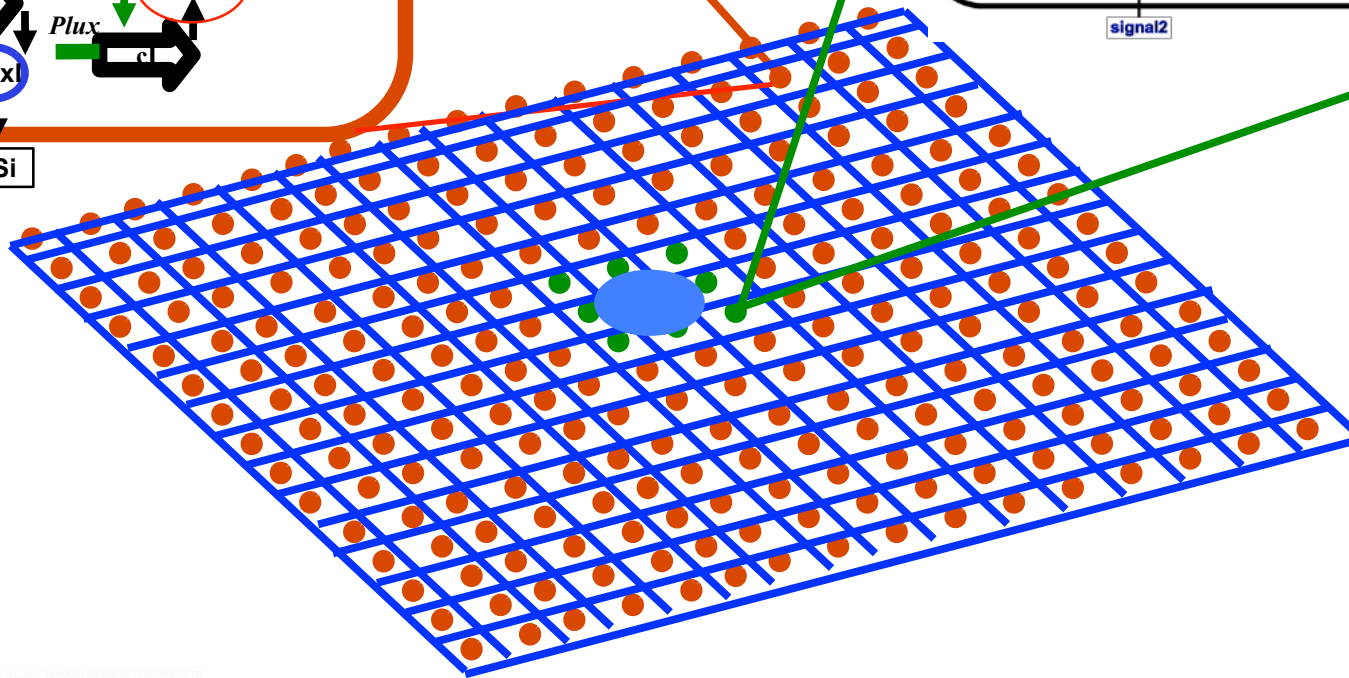
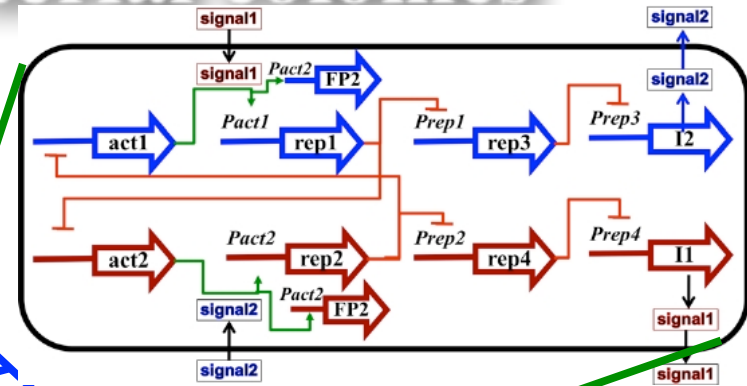
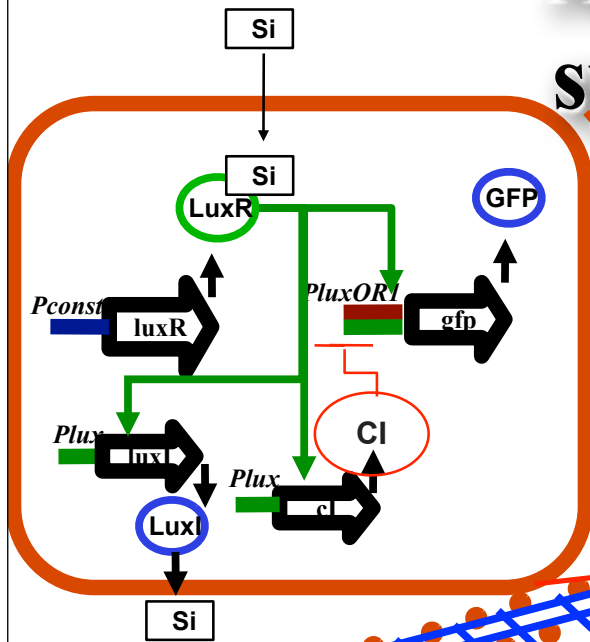


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A Signal Translator for Pattern Formation



Alternating signal pulses in synthetic bacterial colonies



Alternating signal pulses in synthetic bacterial colonies

Simulation III

AlternatingPulses.htm



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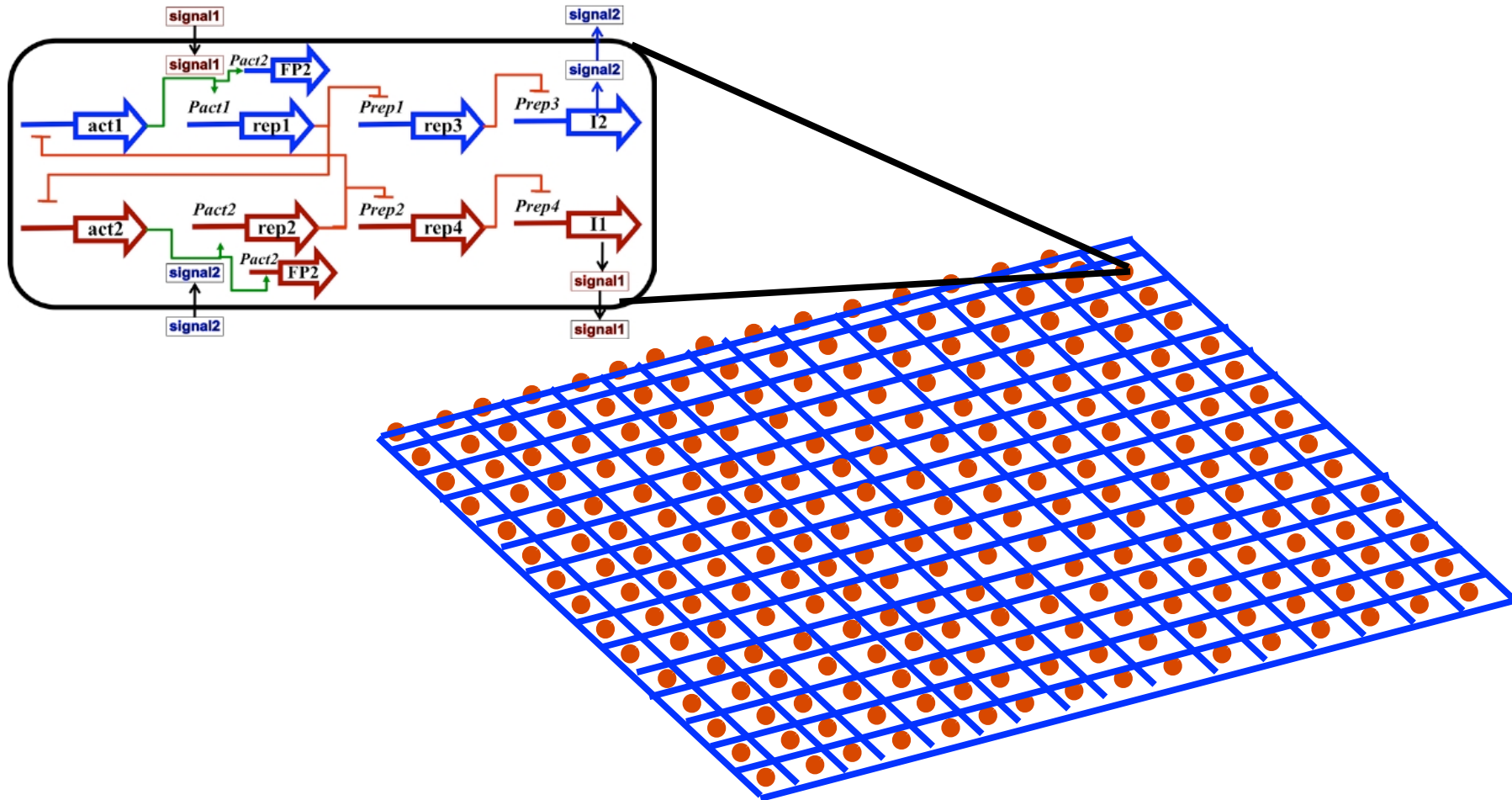


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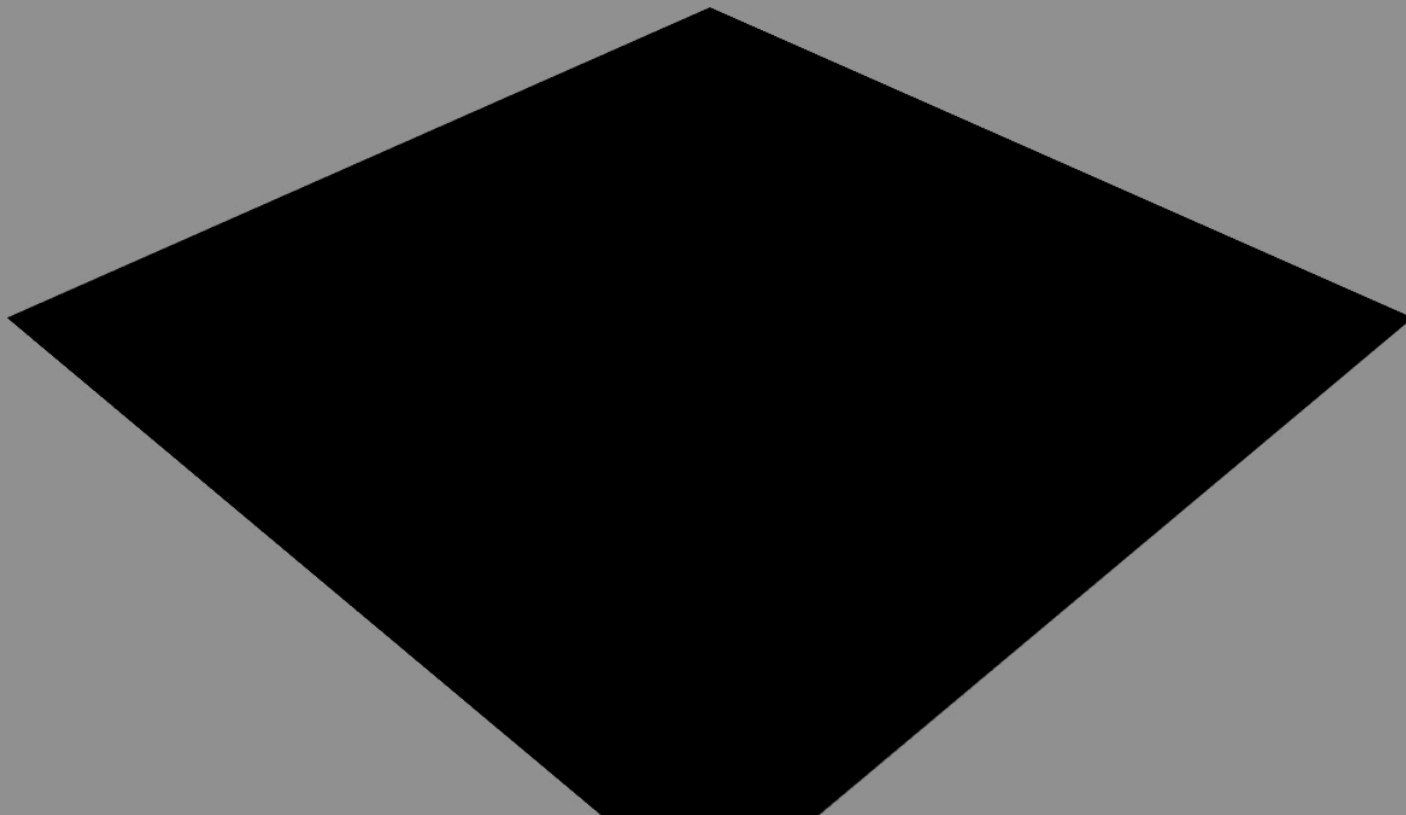
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Uniform Spatial Distribution of Signal Translators for Pattern Formation

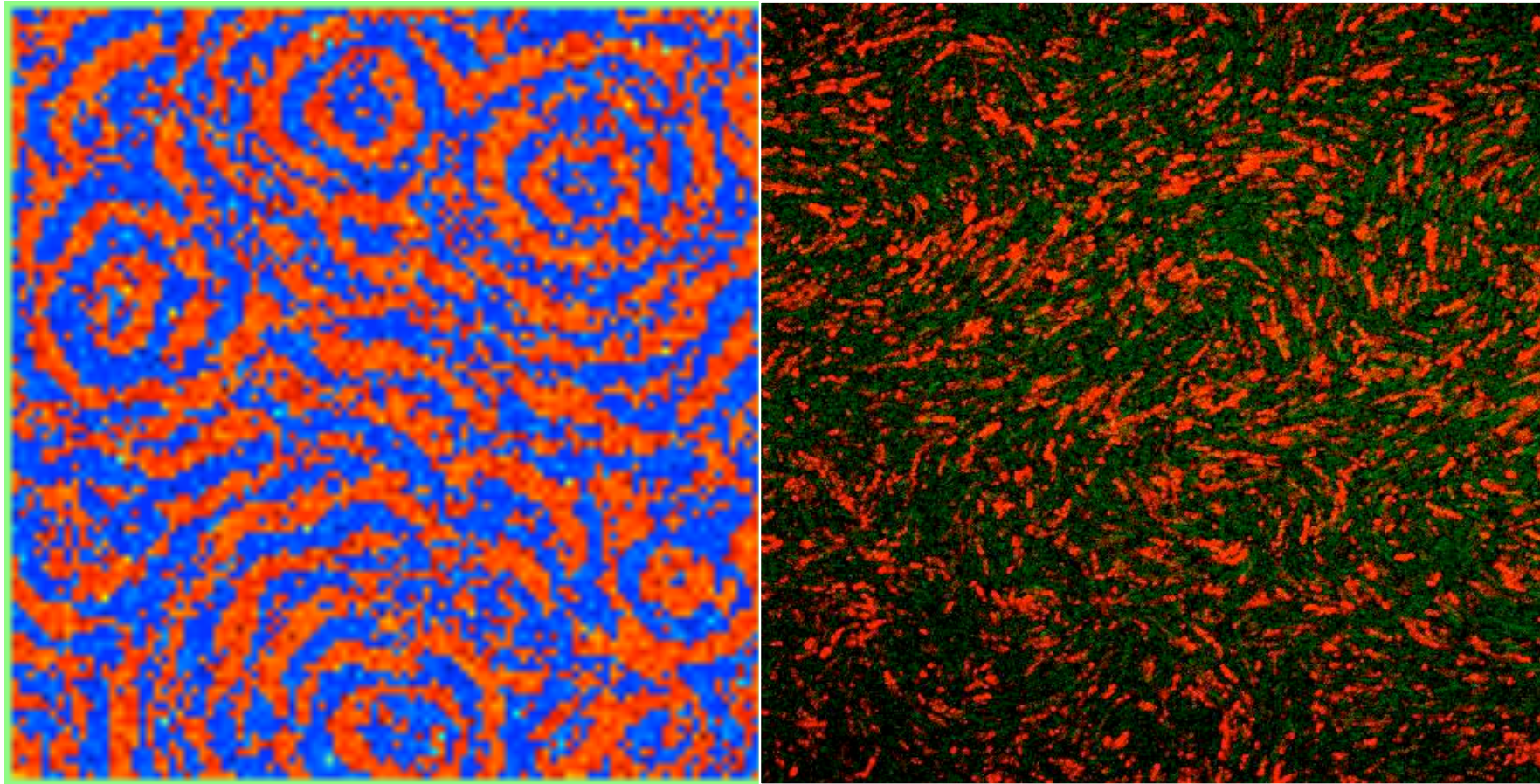


Turing Patterns in Bacterial Colonies

Turing Pattern Formation in a Bacterial Population (0.0 hours)



In Silico & In Vivo



Outline

- The cell as a Computing Device for Biocomputing
- P Systems for Representing Cellular Computation
- Examples of Biocomputation
- **Conclusions**

TAKE HOME MESSAGE

- Living cells as **stochastic & asynchronous** bio-processors that **adapt and generate** their own hardware on-demand
- Information processing is organised via interconnected networks (genes, signaling, metabolic, etc)
- **P systems** are a handy way of specifying *discrete and stochastic rule-based compartmental models for cellular computation*.
- **Modularity in P systems** as a design principle for synthetic networks that enables *reusability, hierarchical abstraction and standardisation*.
- Automated explorations (evolutionary search) on models' structure and parameters.
- Computer Aided analysis of *modular and alternative designs (e.g. synthetic network functionality)*.

Other Sources

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F. Romero-Campero, H.Cao, M. Camara, and N. Krasnogor. Structure and parameter estimation for cell systems biology models. In Maarten Keijzer et.al, editor, Proceedings of the Genetic and Evolutionary Computation Conference (GECCO-2008), pages 331-338. ACM Publisher, 2008. This paper won the Best Paper award at the Bioinformatics track.

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Any Questions?



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